



# **An Approach to Design a New Multifunctional Reversible Logic Gate (MRLG)**

Vinay Kumar, Divya Dhawan

PG Student, Department of ECE, PEC University of Technology, Chandigarh, India

Asst. Professor, Department of ECE, PEC University of Technology, Chandigarh, India

**ABSTRACT:** The problem with Conventional digital circuits is the substantial energy these loss during operation. Therefore these suffer from loss of information bits hence the information itself. So a need for energy minimization was felt not just from efficiency point of view but for the proper functioning of circuit and Reversible circuits have fulfilled this need the best in the domain of digital systems. In this paper we have demonstrated functioning of a New Multifunctional Reversible Logic Gate (MRLG). The proposed MRLG gate is fully reversible and designed with CMOS and pass transistor (PT) logic design technique which has many inherent benefits such as: low power consumption, small delay and area. We have also presented a 16-bit binary logic operation circuit which is designed using a single MRLG unit.

**KEY WORDS:** Reversible logic, CMOS and pass transistor (PT) logic, MRLG gate, 16 -Boolean logical function,

## **I. INTRODUCTION**

Moore's law, that has only outperformed itself in the past, states that, the number of the transistor fabricated in an IC doubles in a period of a year and a half, so does the heat generation arising from the increasing chip density. Hence In the past years the incentives of Reversible logic have become increasingly motivating. During the operation conventional gates dissipate heat on losing a bit. In 1973 C.H Bennett [1], a physicist, demonstrated that when a circuit is designed with reversible logic no energy dissipation takes place. A circuit is reversible if one can recover input data from the output data which means the circuit information is lossless. The general considerations of bijectivity is imposed on the design of reversible logic, which means that the circuit design should have equal number of output and input and one to one mapping. This eliminates the loss of information that is main reason for power dissipation. The unused outputs of reversible gate are called Garbage output similarly Redundant Inputs to reversible gate are called Garbage inputs. Complexity and Performance of reversible circuits/ gate are defined by the following parameters

- ❖ Number of logic gates
- ❖ Number of garbage and constant inputs
- ❖ Number of Garbage outputs.
- ❖ Fan-out is restricted in reversible logic gate. The fan- out of each gate is equal to one. If more fan out are required then use a copying gate.

In the end of this paper we get a new reversible logic gate so as to produce minimum no. of garbage output, lower quantum cost and minimum delay. In Section II we have outlined the related work in terms of quantum cost functionality, number of inputs and outputs. In Section III we have described the proposed New Multifunctional Reversible Logic Gate (MRLG) with CMOS and pass transistor (PT) logic structures. The proposed MRLG gate has been developed to operate in the voltage range of 1.5 V to 5V. The proposed designed gate has length 180nm and width 2 $\mu$ m transistor with gpdk 180 process. Section IV presents the simulation result and discussion. Section V presents the application of MRLG. Conclusion is presented in section VI, and the future scope presented in section VII.

# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

## II. RELATED WORK

Various similar implementation of logic gates have been addressed in [1-14], the classification is defined in terms of its size and functionality. The 1x1 reversible gate is NOT. The 2x2 reversible gate is Feynman. The 3x3 reversible gates are Fredkin, Toffoli, Peres, TR gate, new gate, PRT-1 and PRT-2 and the 4x4 gate includes MKG, TSG and DKG. In Table 1 we have described the logic functionality and a brief description of various gates.

Table 1: Existing Reversible Logic Gates

Reversible Gate (Existing)	Gate Size	Input and output	Functionality	Logic Discription	Quantum cost
Feynman 1985 [ 5 ]	2x2	Input A, B Output P=A and Q = A ⊕ B	Buffer, Ex-OR	Output Q = A' , when input A=1 = Buffer, otherwise	1
Fredkin 1982 [6 ]	3x3	Input A, B, C Output P=A, Q=A'B⊕AC and R=A'C'⊕AB)	C- Swap gate	Output Q = C and R = B when input A = 1. Otherwise Q = B and R = C'.	5
Toffoli 1980 [ 16 ]	3x3	Input A, B, C Output P=A, Q=B and R=AB⊕ C	Buffer, C-Controlled gate	R = C' , When A =1 and B = 1 = Buffer, otherwise	5
Peres 1985[14 ]	3x3	Input A, B, C Output P=A, Q= A⊕ B and R=A⊕ BC	Controlled NOT, CC-NOT, Copying gate	Q = B' , When A=1 R= C' , When A=1 and B=1.	4
TR 2011 [7 ]	3x3	Input A, B, C Output P=AQ= A⊕ B, R=AB'⊕ C	NAND, Buffer	R = A NAND B, when B = inverted input	6
New 2002 [2]	3x3	Input A, B, C Output P=A, Q= AB⊕ C, R=A'C'⊕ B'	Buffer, AND, Ex-OR	R= A' Ex-OR B' , When C=0 Else Q= A AND B	7
PRT-I 2011[15 ]	3x3	Input A, B, C Output P=AB⊕B'C,Q=A⊕ B⊕ C and R=AB'⊕ BC	OR , AND, Ex-OR, Ex-NOR	Q= B Ex- NOR C, and R= B OR C When A=1. and Q= A Ex-OR B, and R= A AND B, When C=0	6
PRT-II 2011 [ 15 ]	3x3	Input A, B, C Output P=BC⊕AC', Q=A'(B⊕C)+AB and R=C	Ex-NOR, OR	P= B OR C, When A=1, and Q= A Ex-NOR C, When C= 1	5
TSG 2005 [ 8 ]	4X4	Input A, B, C, D Output P = A, Q = A' C'⊕ B' , R = (A'C'⊕ B') ⊕ A and S=(A'C'⊕B') D⊕ (AB⊕ C)	AND	S= A AND B, When C=0 & D= 0	14
MKG 2007 [ 11 ]	4X4	Input A, B, C, D Output P = A, Q= C, R = (A'D'⊕ B') ⊕ C and S = (A'D'⊕ B')C ⊕	Buffer, Ex-NOR , Ex-OR	R= B Ex-OR C, and S= B AND C When A=0 & D=0	9

# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

		(AB⊕D))		R= B Ex-NOR C, When A=1 & D= 0	
DKG 2011 [ 10]	4X4	Input A, B, C, D Output P = B, Q = A'C + AD', R=(A⊕B)(C⊕D) ⊕ CD and S = B⊕C⊕ D)	Buffer, Ex-OR	Ex-OR when A=0	11

### III. PROPOSED MULTIFUNCTIONAL REVERSIBLE LOGIC GATE (MRLG)

The basic proposed of this Multifunctional Reversible Logic Gate is a reversible logic gate. MRLG have a low power and small delay in design. Fig.1 was the basic approach of this proposed 4X4 reversible MRLG gate. Table 2 shows the MRLG gate truth table. In the truth table of the MRLG input pattern corresponding to a specific output pattern is determined uniquely and to maintain the one-to-one correspondence mapping between the input vector and the output vector. The MRLG input vector is  $I_v = (A, B, C, D)$  and there output vector is  $O_v = (P = A, Q = AB \oplus A'C, R = B \oplus AC, S = B \oplus AC \oplus D)$ . It basically consists of two modules, one is made by CMOS and other is by PTL (Pass transistor logic). Both techniques have various disadvantages and advantages.

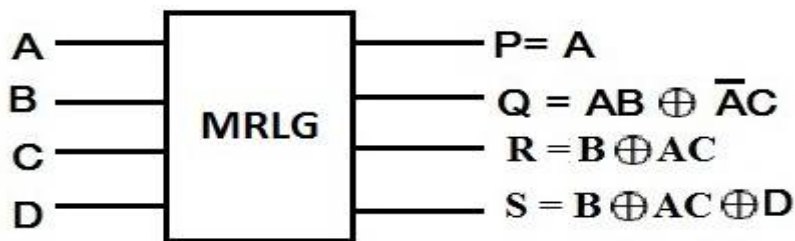


Fig. 1. Proposed MRLG reversible gate.

Table 2: Proposed MRLG gate truth table

Input				Output				Input				Output			
A	B	A	B	C	D	P	Q	A	B	A	B	C	D	P	Q
0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	0
0	0	0	1	0	0	1	0	1	0	0	1	1	0	1	0
0	0	1	0	0	1	0	0	1	0	1	0	1	0	1	1
0	0	1	1	0	1	1	0	1	0	1	1	1	0	0	1
0	1	0	0	0	0	1	1	1	1	0	0	1	1	1	1
0	1	0	1	0	0	0	1	1	1	0	1	1	1	0	1
0	1	1	0	0	1	1	1	1	1	1	0	1	1	0	0
0	1	1	1	0	1	0	1	1	1	1	1	1	1	1	0

#### A. CMOS realization of MRLG gate:

The proposed designed gate is based on PMOS and NMOS transistor width and length ratio 0.180/2 μm and gpdk 180 processes. Fig. 2 represents the CMOS realization of MRLG gate. The first output of the MRLG gate is buffer of the first input. So, with grounded gate a PMOS transistor is used. The second output  $Q=AB \oplus A'C$  is XOR function of the AND function of first and second input with an AND function of complement of first input and third input, the third output  $R=B \oplus AC$  is XOR function of second input with an AND function of the first and third input, and the forth output  $S=B \oplus AC \oplus D$  is XOR function of the third output with forth input. Circuits realized by the pull-up and pull-down networks with PMOS and NMOS transistors respectively. Transistors count in MRLG gate in CMOS realization technique is 49.

# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

## B. Pass transistor realization of MRLG gate:

The Pass transistor logic (PT) realization of MRLG gate is shown in fig.3. Consider the input are  $A= '1'$ ,  $B= '1'$ ,  $C= '0'$  and  $D= '1'$ . Since  $A= '1'$  the transistor  $Q1$  is OFF and  $Q2$  is ON. So the output  $P= '1'$ . Since  $A= '1'$ ,  $B= '1'$  and  $C= '0'$ ,  $Q4, Q7, Q10$  are ON and  $Q3, Q5, Q6, Q8, Q9$  are OFF So the output  $Q= '1'$ . And  $Q12, Q13, Q16$  are ON and  $Q11, Q14, Q15$  are OFF, so the output  $R= '1'$ . Since  $A= '1'$ ,  $B= '1'$ ,  $C= '0'$  and  $D= '1'$ ,  $Q17, Q20$  are ON and  $Q18, Q19$  are OFF. So the output  $S= 0$ . Transistors count in MRLG gate in CMOS realization technique is 20.

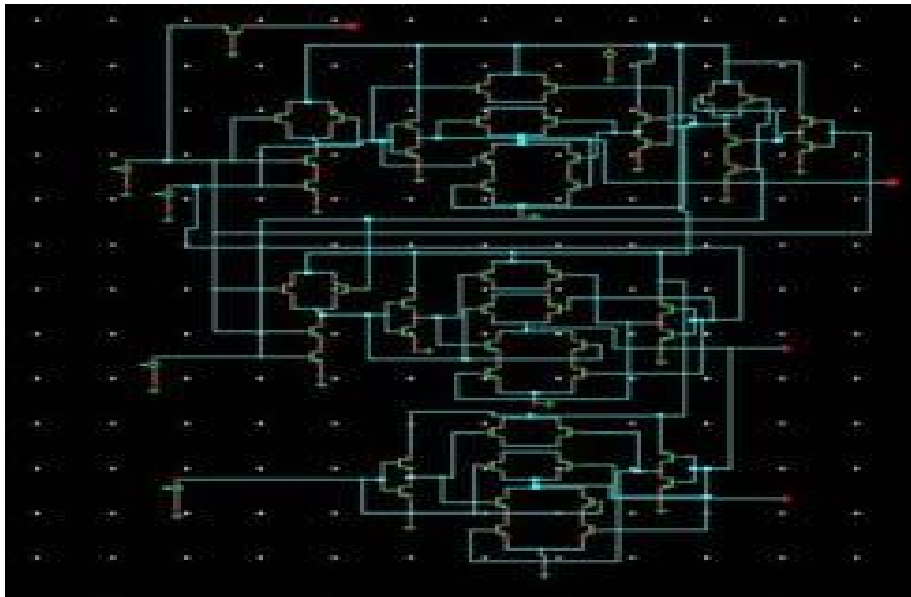


Fig. 2. CMOS realization of MRLG gate

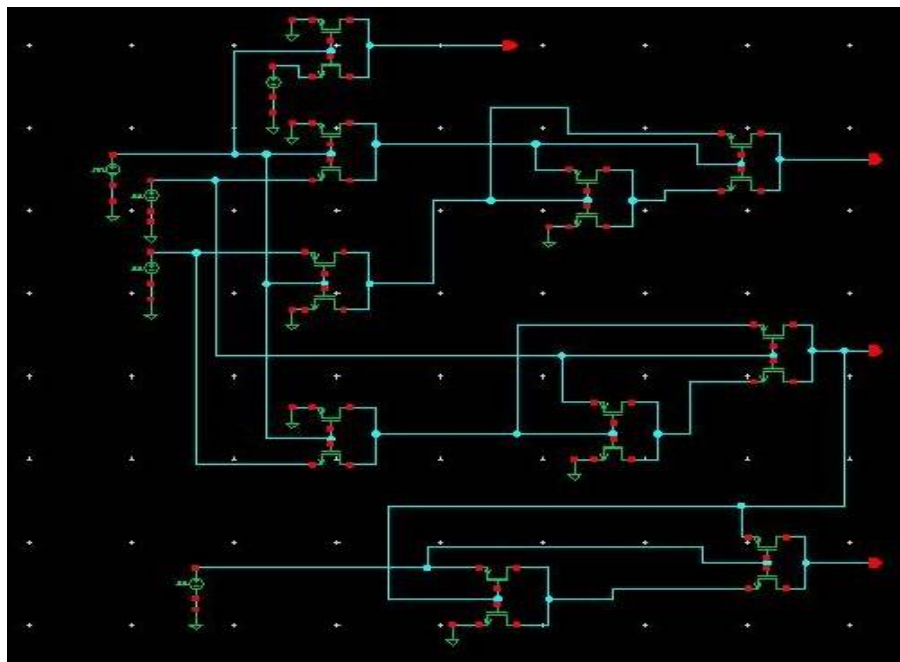


Fig. 3. Pass transistor realization of MRLG gate

# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

## IV. RESULT AND DISCUSSION

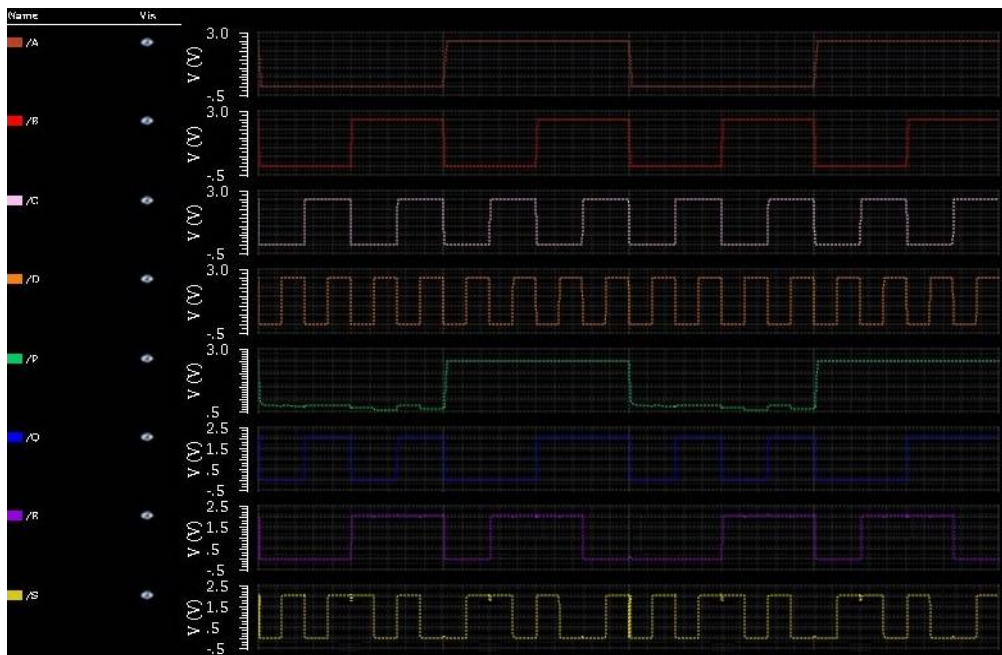


Fig. 4. Input output waveform of MRLG gate

Table 3 and Table 4 give the output parameters and the comparisons between the Pass transistor logic and CMOS realization of MRLG gate. In this paper observed the propagation delay for all input to all output like  $A \rightarrow P$ ,  $A \rightarrow Q$ ,  $A \rightarrow R$ ,  $A \rightarrow S$ ,  $B \rightarrow P$ ,  $B \rightarrow Q$ ,  $B \rightarrow R$ ,  $B \rightarrow S$ ,  $C \rightarrow P$ ,  $C \rightarrow Q$ ,  $C \rightarrow R$ ,  $C \rightarrow S$ ,  $D \rightarrow P$ ,  $D \rightarrow Q$ ,  $D \rightarrow R$  and  $D \rightarrow S$ . In Table 3 tabulated the average of propagation delay of MRLG gate for applied voltage in different design techniques (CMOS and Pass transistor logic) for inputs A, B, C and D to Output P, Q, R, and S.

Table 3. Delay of MRLG gate for applied voltage in different design techniques (CMOS and Pass transistor logic)

	CMOS Logic					Pass Transistor Logic			
	Voltage applied	1.5	2	2.5	3	1.5	2	2.5	3
Delay 1 (ns)	A to P	23.74	23.8	23.79	48.89	.2110	.5385	.4447	.3730
	A to Q	.3866	.5728	.7254	.9025	.4734	.5385	.4910	.5338
	A to R	.628	.8941	1.025	1.135	49.91	36.42	11.25	1.04
	A to S	1.119	1.18	1.22	1.25	.7738	.8953	.9879	.9235
	Avg.	6.4684	6.6117	6.6901	13.044	12.842	9.5980	3.2934	.7175
Delay 2 (ns)	B to P	24.46	24.52	24.5	49.61	.7743	1.189	1.165	1.14
	B to Q	.3334	.1472	.0054	.2005	.0599	.2211	.2290	.2329
	B to R	.09129	.1741	.3048	.415	56.46	37.50	11.97	.2735
	B to S	.3992	.4602	.5002	.529	.2405	.2453	.2679	.1568
	Avg.	6.3209	6.3253	6.326	2.6886	14.384	9.7888	3.4079	.4508
Delay 3 (ns)	C to P	24.82	24.88	24.86	49.97	1.011	1.514	1.525	1.529
	C to Q	.6934	.5872	.3546	.1595	.3266	.5491	.187	.6162
	C to R	.4513	.1859	.0552	.05512	50.71	37.4	12.33	.1098
	C to S	.03923	.1002	.1402	.1695	.0262	.0797	.0921	.2265
	Avg.	6.509	6.4383	6.3525	12.018	5.8857	9.8857	3.5335	.6203
D to P	25.0	25.06	25.04	15.15	1.144	1.677	1.671	1.715	



# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

Delay 4 (ns)	D to Q	.8734	.6872	.5346	.3395	.4596	.7112	.7440	.7690
	D to R	.6313	.3659	.2552	.1249	50.85	36.56	36.56	12.51
	D to S	.1408	.0784	.0398	.01046	.1565	.2422	.2721	.2721
	Avg.	8.8349	6.5479	6.4674	3.9062	13.153	9.7976	9.8110	3.816
<b>Total delay (ns)</b>		<b>7.0333</b>	<b>6.4808</b>	<b>6.459</b>	<b>7.9142</b>	<b>11.566</b>	<b>9.7675</b>	<b>5.0115</b>	<b>1.4011</b>

In Table 4. Shows the average power dissipation calculated for the entire input bit pattern. In comparison of different techniques, the advantage of this design is not only depends on transistor count, delay, and power but also on AT (transistor count (area) and delay product) and PDP (power and delay product) values. The comparisons of transistors count, Power dissipation, Delay, PDP and AT are shown in Table 4.

Table 4. Synthesis results of MRLG using CMOS and Pass transistor logic

Revisable gate	Logic family	No. of transistors required	Voltage applied	Power dissipation (watts)	delay (ns) (average)	Power delay product	Area delay product
MRLG	CMOS	49	1.5	15.64u	7.0333n	109.996f	344.631
			2	34.55u	6.4808n	223.912f	317.559
			2.5	88.55u	6.4590n	571.945f	316.491
			3	365.9u	7.9142n	2895.81f	387.795
	Pass Transistor logic	20	1.5	19.44u	11.566n	224.843f	231.320
			2	294.8u	9.7675n	2879.46f	195.350
			2.5	558.3u	5.0115n	2797.92f	100.230
			3	1.414m	1.4011n	1981.16f	028.022

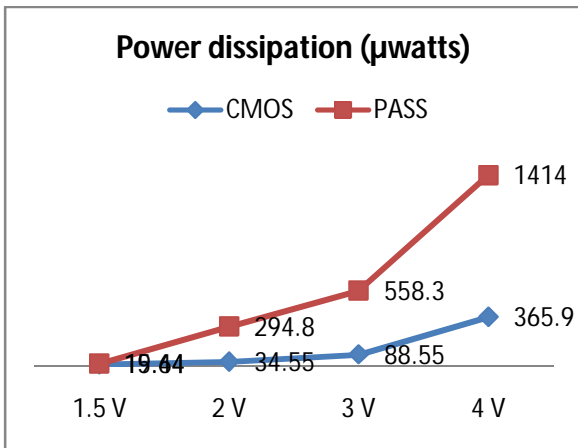


Fig. 5. Power analysis of MRLG gate.

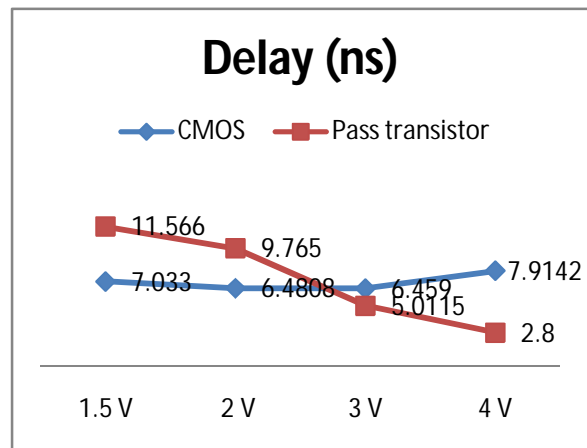


Fig. 6. Delay analysis of MRLG gate

## V. APPLICATION OF MRLG GATE

By using MRLG gate we can do design 16 Boolean logical operations. We know that Binary logic (Base = 2) has two logical states 0 and 1. Depending on the number of used variables and base, different logic functions can be generated. The number of possible Boolean function is [17]

$$N = B^{B^n}$$

Where n is the number of variables and B is the Base. In binary logic (B=2) of two variables (n=2), the no. of Boolean function is  $N = B^{B^n} = 2^{2^2} = 16$ . Table 5.shows the all possible Boolean functions of two variables.

# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

Table 5. Sixteen Boolean Logical Functions (F1-F16).

Input	A	0	0	1	1	Output	Input	A	0	0	1	1	Output
	B	0	1	0	1			B	0	1	0	1	
Output	F1	0	0	0	0	False (0)	Output	F9	1	0	0	0	A'B'
	F2	0	0	0	1	AB		F10	1	0	0	1	A B
	F3	0	0	1	0	AB'		F11	1	0	1	0	B'
	F4	0	0	1	1	A		F12	1	0	1	1	A+B'
	F5	0	1	0	0	A'B		F13	1	1	0	0	A'
	F6	0	1	0	1	B		F14	1	1	0	1	A'+B
	F7	0	1	1	0	AB		F15	1	1	1	0	A'+B'
	F8	0	1	1	1	A+B		F16	1	1	1	1	True (1)

We can apply any one of the light sources A, B, 0 (zero power supply), or 1 (constant power supply) to the all 4 inputs (A, B, C, and D) of the MRLG gate, we get all sixteen Boolean operations as shown in Table 5 according to Fig. 7 (a)–(h).

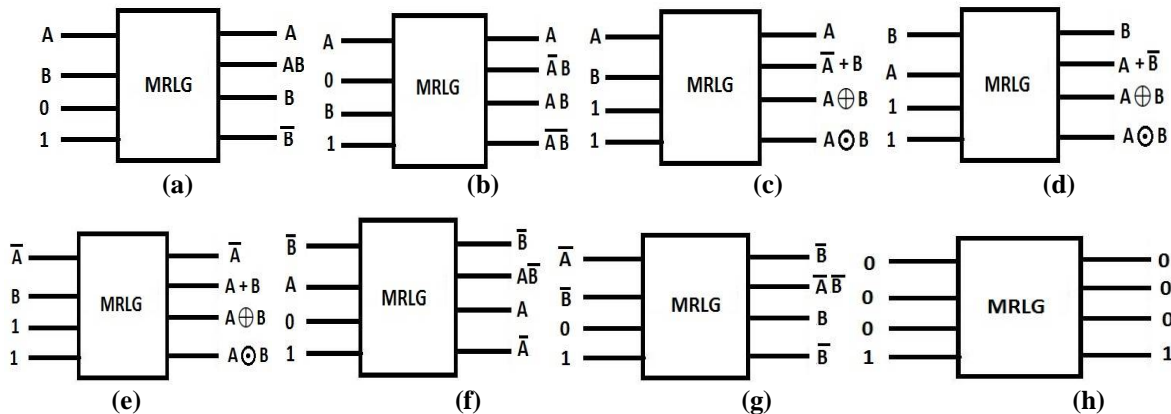


Fig. 7. 16- Boolean logical operations

## VI. CONCLUSION

In this paper approach to design of new reversible logic 4x4 Multifunctional Reversible Logic Gate. Circuits are implemented in transistor level with different design techniques Pass transistor logics (PT) and CMOS. And compare their performance by different supply voltage 1.5 to 4 V (1.5V, 2V, 3V, 4V). In this paper Conclude that the design of a multifunctional reversible gate for a reversible digital designs that can be minimizing the power consumption, delay, garbage outputs and quantum cost. After that, we observe a different property of the reversible MRLG gate in compare to the other alternative reversible gate. MRLG can design sixteen Boolean logical operations. Fig.7. Shows the sixteen Boolean operations and clear that in this case there in no garbage.

## VII. FUTURE SCOPE

Due to all logical operation (16) and minimum power delay product (PDP) this MRLG can be used to design Adder Subtractor, Multiplier, Compressor, Parity Generator and Checker, Multiplexer, Demultiplexer, Decoder, Latch, Flip-flop, Counter, sequence generator, sequence counter, etc circuits.



# International Journal of Innovative Research in Computer and Communication Engineering

(An ISO 3297: 2007 Certified Organization)

Vol. 4, Issue 5, May 2016

## REFERENCES

1. Bennett, C.H., "Logical Reversibility of Computation", IBM Journal Research and Development, 525-532. 1973.
2. Azad Khan, M.H., "Design of Full-Adder with Reversible Gates", International Conference on Computer and Information Technology, Dhaka, Bangladesh, pp: 515-519. 2002.
3. Bisdounis, L., D. Gouvetas and O. Koufopavlou, "A comparative study of CMOS circuit design styles for low-power high-speed VLSI circuits". International Journal of Electronics, 599-613. 1998.
4. Chatzigeorgiou, A. and S. Nikolaidis, "Modeling the operation of pass transistor and CPL gates", International Journal Electronics, 977-1000, 2001.
5. Feynman, R., "Quantum Mechanical Computers", Optic News, 11-20, 1985.
6. Fredkin, E. and T. Toffoli, "Conservative Logic", International Journal of Theoretical Physics. 219-253. 1982.
7. Himanshu Thapliyal and Nagarajan Ranganathan, "A New Design of the Reversible Subtractor circuit", 11<sup>th</sup> IEEE international Conference Nanotechnology, 2011.
8. Himanshu Thapliyal and M.B. Srinvas, "Novel Reversible TSG gate and Its Application for Designing Components of Primitive Reversible/Quantum ALU", ICICS 2005.
9. Krishnaveni, D. and M. Geetha Priya, "Design of Reversible Serial and Parallel Novel Adder/Subtractor", International Journal of Engineering Science and Technology; (IJEST) march. 2011.
10. Landauer, R., "Irreversibility and Heat Generation in the Computing Process", IBM Journal Research and Development, 183-191, 1961.
11. Majid haghparast and Keivan Navi, "A Novel Reversible Full Adder Circuit for Nanotechnology Based Systems", Journal of Applied Sciences, 3995-4000, 2007.
12. Maslov, D., D.M. Miller and. G.W. Dueck, "Techniques for the Synthesis of Reversible Toffoli Networks", ACM Transaction Design Automated Electronic System, 2007.
13. Morgenshtein, A. A. Fish and I.A. Wagner, "Gate-diffusion input (GDI): A power-efficient method for digital combinatorial circuits", IEEE Transaction on VLSI, 566-581, 2002.
14. Peres, A., "Reversible Logic and Quantum Computers", Physical Review, 3266-3276. 1985.
15. Rashmi, S.B. and B.G. Tilak, "Transistor Implementation of Reversible PRT gates", International Journal of Engineering Science and Technology, 2011.
16. Toffoli, T., "Reversible Computing", Tech Memo MIT/LCS/TM-151, MIT Lab for Computer Science, 1980.
17. R. Cunha, H. Boudinov, and L. Carro, "Quaternary look-up tables using voltage-mode CMOS logic design," in Proc. 37th Int. Symp. Multiple Valued Logic (ISMVL'07), p. 56.

## BIOGRAPHY



Vinay Kumar pursuing M.E in the branch of Electronics VLSI Design at PEC University of Technology Chandigarh, India.



Mrs. Divya Dhawan is currently working as Asst. Professor in ECE Department of PEC University of Technology Chandigarh, India. She has a teaching experience of nearly 18 years. She is a member of IEEE, ISTE, and IET. Her research interests include Optical Communication, Photonics Systems and Digital system design.