

Frequent Pattern Mining Using Hyper Path in Hypergraphs

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ABSTRACT: Hypergraph is used as a tool to model and solve some classes of problems arising in frequent pattern mining. Hypergraph is a generalization of a graph wherein edges can connect more than two vertices and are called hyperedges. Efficient algorithms for generating the hypergraph model and extracting frequent patterns for association rule mining are proposed in this paper. An algorithm is introduced which generates the Hypergraph model D and which also simultaneously computes several other measures such as frequent items, nonfrequent items, total number of hyperedges, length of a largest transaction, frequency of occurrence of various nodes and the number of occurrences of each hyperedge in D . The second algorithm generates all the patterns of the transaction database using the above data structure. This algorithm can be modified to extract frequent patterns. The third algorithm deals with extraction of frequent subhypergraphs induced by all frequent patterns L . The study shows that this new approach has high performance in various kinds of data, which outperforms the previously developed algorithms in different settings, and is highly scalable in mining different databases.

KEYWORDS: frequent pattern, hypergraph, hyperedge, hyperpath, association rule, path system, transaction database,

I. INTRODUCTION

A hypergraph introduced by Berge C [1] is a set V of vertices and a set of non-empty subsets of V , called hyper edges. Unlike graphs, hypergraphs can capture higher-order interactions in social and communication networks that go beyond a simple union of pair wise relationship. Just as graphs naturally represent many kinds of information in mathematical and computer science problems, hypergraphs also arise naturally in important practical problems, including circuit layout, numerical linear algebra, etc. A hypergraph is a natural extension of a graph obtained by removing the constraint on the cardinality of an edge: any non-empty subset of V can be an element (a hyper edge) of the edge set E (see Figure 1). For example, let $X = \{x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8\}$ and $E = \{E_1, E_2, E_3, E_4, E_5, E_6\} = \{\{x_3, x_4, x_5\}, \{x_5, x_8\}, \{x_6, x_7, x_8\}, \{x_2, x_3, x_7\}, \{x_1, x_2\}, \{x_7\}\}$. This hypergraph is given in Figure 1.

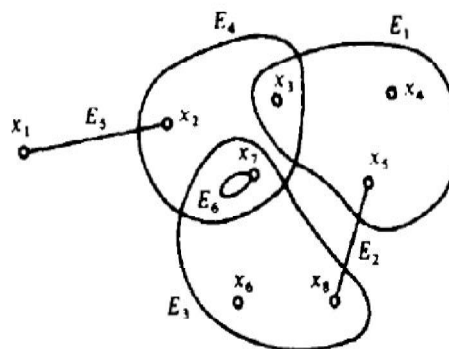


Figure 1 Hypergraph

A hypergraph is also called a set system or a family of sets drawn from the universal set X . The difference between a set system and a hypergraph (which is not well defined) is in the questions being asked. Hypergraph theory



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tends to concern questions similar to those of graph theory, such as connectivity and colorability, while the theory of set systems tends to ask non-graph-theoretical questions.

II RELATED WORK

The problem of mining frequent itemsets arose first as a sub problem of mining association rules Agrawal et al (1993). The frequent itemset mining problem has been formulated as the computational relevant step in association rule mining. Frequent itemset mining problem appears as a sub problem in many other data mining fields like association rule discovery[10], correlations, classification [11] clustering [12], web mining [13] and [14]. The original motivation for searching association rules came from the need to analyse the supermarket transaction data, that is, to examine customer behavior in terms of the purchased products. Association rules describe how often items are purchased together. For a given sequence of itemsets, we have to find itemsets that are contained as a subset in more than a given number of elements of the sequence.

III. HYPERGRAPH AND HYPERPATH

Let V be a finite set and E a family of subsets of V . If $E_i \neq \phi$ and $\bigcup_{E_i \in E} E_i = V$ then the couple $D = (V, E)$ is called a hypergraph. Each element $v \in V$ is called a vertex and each element $E_i \in E$ a hyperedge. A hyperpath between two vertices u and v is a sequence of hyperedges $\{E_1, E_2, \dots, E_m\}$ such that $u \in E_1$, $v \in E_m$ and $E_i \cap E_{i+1} \neq \phi$ for $i=1, 2, \dots, m-1$. A hyperpath is simple if non-adjacent hyperedges in the path are non overlapping, that is, $E_i \cap E_j = \phi$, $\forall j \neq i, i \pm 1$. Obviously any transaction database is a hypergraph. The items are the vertices and any transaction is a hyperedge. This hypergraph denoted by $D = (I, T)$.

IV. HYPERGRAPH MODEL FOR TRANSACTION DATABASE

Let $T \in D$ and $X \subset I$. Then T supports X if $X \subset T$, the support of X , denoted by $f(X)$ defined as $f(X) = \frac{| \{T \in D | X \subset T\} |}{|D|}$. For a minimum threshold $s \in [0, 1]$, $X \subset I$ is a frequent pattern if $f(X) \geq s$. An association rule is an implication of the form $X \Rightarrow Y$, where $X \subset I$, $Y \subset I$ and $X \cap Y = \phi$. The support of the rule $X \Rightarrow Y$ is $f(X \cup Y) = \frac{| \{T \in D | X \cup Y \subseteq T\} |}{|D|}$. The confidence of the rule $X \Rightarrow Y$ is $Conf(X \Rightarrow Y) = \frac{f(X \cup Y)}{f(X)}$.

The hypergraph model can be built easily, $D = (I, TDB)$. Each transaction corresponds to an edge, the number of distinct items is the order of D , and the number m of transactions is size of D . Since every item belongs to at least one transaction, D is a hypergraph in the classical sense (that is without isolated vertices). The number of transactions to which an item i belongs (frequency of i) is $d_D(i)$, the degree of i in D . The maximum length of a transaction in TDB is the rank of D . It is defined as $\gamma(D) = \max \{ |T| : T \in D \}$ [2]. In this paper a data structure is proposed which consists of a hypergraph D and a system of hyperedges in D for representing a transaction database. The vertex set of the hypergraph is the item set I . Any transaction T of the form $\{x\}$ is represented as a loop at x .

V. ALGORITHM FOR CONSTRUCTING HG MODEL FOR A TDB

In this section an algorithm is introduced to construct the hypergraph representing a TDB. The algorithm scans the database exactly once, dynamically constructs the hypergraph D and simultaneously computes several parameters such as frequency of occurrence of each node, number of loops at each node, number of occurrence of each hyperedge, total number of hyperedges in D and maximum length of a transaction[3].

The algorithm first creates all nodes of D , one node for each item, with support count 0. Then each transaction in the transaction database is scanned and hyperedge representing that transaction is constructed. If (i_1, i_2, \dots, i_k) is a transaction, the hyperedge is represented as a linked list. The header of this list has two fields. One field is used to store the list of vertices (i_1, i_2, \dots, i_k) which is called the label of the hyperedge and the other field is used to store the



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occurrence frequency of the hyperedge. Dynamic memory allocation method is used for storing these values. The pseudo code for the construction of hypergraph is given in Figure 3.

Algorithm: Construction of Hypergraph Model, D for a TDB

Input : TDB, Transaction Database

I , set of items in TDB

Output:

D , Hypergraph of given TDB

n , Order of D

$\gamma(D)$, Rank of D

$\delta(D)$, Antirank of D

$f(E_i)$, Frequency of E_i

$starD(i)$, Partial hypergraph formed by the edges containing i , $i \in I$

$V(E_i)$, Set of vertices in the edge E_i

$d_D(i)$, support count or degree of vertex, $i \in I$

$\Delta(D)$, Maximum degree of D $\nabla(D)$, Minimum degree of D

Method:

$E = \phi, m = 0;$

for each $i \in I$,

 CreateNode (i);

end for

for each $T_j \in TDB$

if ($T_j = E_i \in E$) // E is the set of edges in D created so far.

$++ f(E_i)$, // increment the edge count of E_i by 1.

else

 CreateEdge (E_j)

$f(E_j) = 1;$

$V(E_j) = T_j;$

$E = \cup \{E_j : f(E_j)\}$

$m++;$ //find number of distinct edges

end if

end for

$n = |I|;$

$\gamma(D) = \text{Max}_j |E_j|;$

$\delta(D) = \text{Min}_j |E_j|;$

if ($\gamma(D) = \delta(D)$,

return the given TDB is uniform;

end if

for each $i \in I$,

$starD(i) = \{E_j | (E_j \in E) \& (i \in E_j)\}$

end for

for each $i \in I$,

$d_D(i) = \sum_{\forall E_j \in starD(i)} f(E_j)$

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end for

$$\Delta(D) = \text{Max}_{i \in I} (d_D(i))$$

$$\nabla(D) = \text{Min}_{i \in I} (d_D(i))$$

Return D , Hypergraph of TDB

Figure 3 A greedy algorithm for constructing the HG model

The algorithm in Figure 3 is illustrated with a dataset of diseases where a person is suffering from cold, fever and other related symptoms. The real time data set of seasonal fever is collected from the local doctors of Ramachandra Medical College, Chennai which consists of six attributes as {cold, headache, fever, bodypain, allergy, cough} given in Table 1

Table 4.1 Disease dataset

Patient Id	Symptoms
01	Cold, Fever and Allergy
T002	Cold, Headache and Cough
T003	Cold, Headache, Body pain and Fever
T004	Fever, Body pain and Cough
T005	Cold, Fever, Headache and Cough
T006	Cold, Body pain and Cough
T007	Cold, Allergy and Cough
T008	Cold, Cough and Body pain
T009	Cold and Cough
T010	Cold, Headache and Fever

Table 2 Discretised value for symptoms

Symptoms	Discretised Value
Allergy	1
Body pain	2
Cold	3
Cough	4
Fever	5
Head ache	6

Different patients may have different combinations of symptoms. The algorithm in Figure 2 is applied to find the association among the attributes with discretised dataset in the Table 2 of the above Table1[4]. HG model of the TDB of disease data set in Table 3 is shown in the Figure 4.

Table 3 TDB of the disease data set

Patient Id	Items	Patient Id	Items
T001	3, 5, 1	T006	3,2,4
T002	3,6,4	T007	3,1,4
T003	3,6,2,5	T008	3,4,2
T004	5,2,4	T009	3,4
T005	3,5,6,4	T010	3,6,5

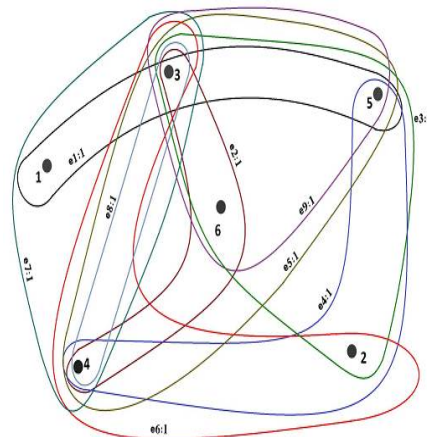


Figure 4 HG model D for TDB in Table 3



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V. MINING OF FREQUENT PATTERNS FROM HG MODEL

In this section an algorithm for extracting the set of all frequent patterns L from a HG model constructed in Section IV is proposed. This algorithm is used to traverse all the hyperedges and extracts all the frequent patterns. The pseudo code for extracting frequent patterns is shown in Figure 5.

Algorithm for Extracting Frequent Patterns from HG Model

The pseudo code for extracting frequent patterns from HG model of a transaction database is given in Figure 5.

Algorithm: Extraction of frequent patterns

Input: D , HG model of TDB
 s , minimum support threshold

Output: L , set of all frequent patterns

Method:

$L = C = \phi$

for each $E_i \in E$ in hypergraph D

$S =$ Set of nonempty subsets of E_i

for each $S_j \in S$ **do**

$f(S_j) = f(E_i)$

if ($S_j \notin L$)

if ($S_j \notin C$)

if ($f(S_j) \geq s$)

$L = L \cup \{S_j : f(S_j)\}$

else

$C = C \cup \{S_j : f(S_j)\}$

end if

else

Add $f(S_j)$ to the count of identical set in C

if ($f(S_j) \geq s$)

$L = L \cup \{S_j : f(S_j)\}$

$C = C - \{S_j : f(S_j)\}$

end if

end if

Add $f(S_j)$ to the count of identical set in L

end if

end for

end for

return L

Figure 5 Pseudo code for extracting frequent patterns from HGmodel of a transaction database.

The set of all frequent patterns generated from the above HGmodel is given in the Table 4. Here the minimum support is assumed as $s = 20\%$.

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Table 4 Frequent patterns generated from the HGmodel in Figure .4 with $s=20\%$

S.No.	Frequent Patterns	Frequency	S.No.	Frequent Patterns	Frequency
1	{3}	9	12	{6,4}	2
2	{5}	4	13	{3,6,4}	2
3	{1}	2	14	{2}	3
4	{3,5}	4	15	{3,2}	4
5	{3,1}	2	16	{6,5}	3
6	{5,1}	2	17	{2,5}	2
7	{3,5,1}	3	18	{3,6,5}	3
8	{6}	4	19	{5,4}	2
9	{4}	6	20	{2,4}	2
10	{3,6}	4	21	{3,2,4}	2
11	{3,4}	6			

Strong association rules can be generated from the set of frequent patterns mined from the given TDB. An association rule which satisfies both minimum support threshold and minimum confidence threshold is called a strong association rule. For each frequent pattern X and for each nonempty proper subset Y of X the algorithm computes the support and confidence of the association rule $Y \Rightarrow X - Y$.

For example from Table 4, $X = \{3, 6, 5\}$ is a frequent pattern with frequency 3. The set of all association rules generated from this pattern with the confidence and support for each rule is given in Table 5. The minimum confidence threshold c and the minimum support threshold s are taken as 75% and 20% respectively.

Table 5 Association rules mined from the frequent pattern {3, 6, 5}.

Sl.No.	Association Rules	Confidence of the Rule	Support of the Rule	R / R'
1	$\{3\} \Rightarrow \{6,5\}$	33 %	33 %	R'
2	$\{6\} \Rightarrow \{3,5\}$	75 %	33 %	R
3	$\{5\} \Rightarrow \{3,6\}$	75 %	33 %	R
4	$\{3,6\} \Rightarrow \{5\}$	75 %	33 %	R
5	$\{3,5\} \Rightarrow \{6\}$	75 %	33 %	R
6	$\{5,6\} \Rightarrow \{3\}$	100	33 %	R

For the TDB given in Table 3 of the disease dataset, 21 frequent patterns are generated. The number of frequent patterns generated with various support counts is given in Table 4. Various association rules generated from the frequent items set {3, 6, 5} is given in Table 5. One of the association rules is $\{5,6\} \Rightarrow \{3\}$ [confidence=100, support=30 %], the information that the patient who is suffering from the disease Fever and Head ache also tend to have the disease Cold. A support of 33 % for association rule means that 33% of all the patients under analysis suffering from the diseases Fever, Head ache and Cold together. A confidence of 100% means that 100% of patients suffering from Fever and Head ache also suffer from Cold. The number of association rules generated from the above disease data set is 51.

VI. RESULTS AND DISCUSSION

For the experimental purpose we have used datasets of different applications. These datasets were obtained from UCI repository of machine learning databases (<http://www.ics.uci.edu/ml/learn/MLRepository.html>-1998). The characteristics of the datasets selected for the experiment are given in Table 6.

Table 6 Data sets used in the analysis

Files	Number of Records	Number of Columns
Adult.D14.N48842.C2.num	48842	14
Hepatitis.D19.N155.C2.num	155	19
Heart.D75.N303.C5.num	303	75
Census	48842	14
LetRecog.D106.N20000.C26.num	20000	17
MushroomD.90.N81424.C2.num	8124	23

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To study the strategies we have conducted several experiments on a variety of data of different sizes and comparing our approach with the well-known SaM algorithms, and FI- tree algorithm. The performance metrics in the experiments is the total execution time taken and the support count for adult, hepatitis and heart datasets. For this comparison also same datasets were selected as for the above experiment with 30% to 70% of minimum support threshold. The experiments were conducted on 2.6 GHz CPU machine with 3 Gbytes of memory using Windows XP operating system. Time needed to mine frequent itemset for different algorithms using the data set given in Table 6 is discussed below.

Table 7 Time scalability with respect to support on the Adult dataset

Support in %	Time in seconds		
	FI-Tree	SaM	HG model
30	8.12	9.85	4.03
40	5.69	6.72	2.08
50	3.56	4.51	1.5
60	1.99	2.69	1.1
70	1.01	1.7	0.8

Time taken to mine frequent pattern with various support threshold on Adult data set is given in the Table 7. The total execution time for our HG model is very much less than that of FI-Tree and SaM methods[9]. The SaM algorithm and FI-Tree algorithms take more time see Figure 6 as that compared to our approach.

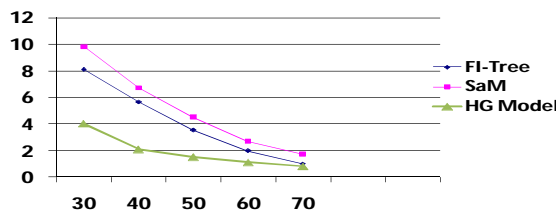


Figure 6 Time scalability with respect to support on the Adult dataset

The total execution time for our new approach HG model and the other algorithms FI-Tree and SaM on Heart data set given in Table 8, algorithms large reduces with the increase in support threshold from 30% to 70%. Our proposed approach takes less time as that compared to the other two algorithms Sam and FI-Tree[7][8]. The execution time of HG model approach with SaM algorithms for hepatitis data set is given in Table 9

Table 8 Run time comparisons on Heart data set

Support in %	Time in seconds		
	FI-Tree	SaM	HG model
30	0.05	0.07	0.035
40	0.4	0.06	0.031
50	0.3	0.05	0.028
60	0.03	0.03	0.02
70	0.01	0.02	0.009

Table 9 Run time comparisons on Hepatitis Data set

Support in %	Time in seconds		
	FI-Tree	SaM	HG model
30	0.64	0.91	0.538
40	0.09	0.28	0.08
50	0.04	0.06	0.03
60	0.03	0.04	0.028
70	0.00	0.0	0.0

A detailed analysis to assess the performance of the algorithm HG- Model with respect to other frequent itemset mining algorithms is conducted. The performance matrix in the experiments is the total execution time taken and the number of item sets generated for different data sets[5][6]. The following performance analysis graphs Figure 7 shows

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the execution time for the algorithms FP-Growth, Eclat, Relim, SaM with the new approach HG Model. Figure 8 shows performance analysis of our approach with other methods. This shows our method outperforms the others approaches.

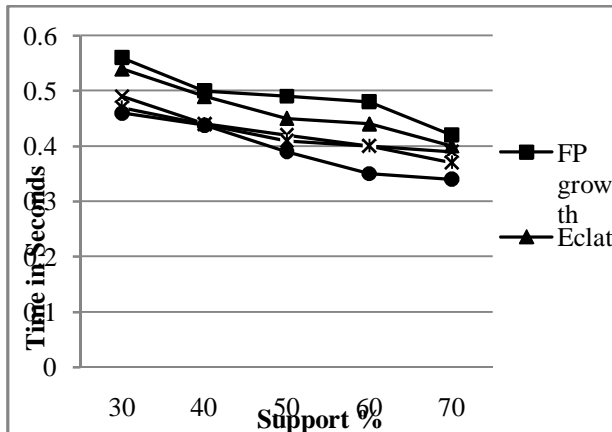


Figure 7 Comparison of execution time of the algorithms on Adult data set.

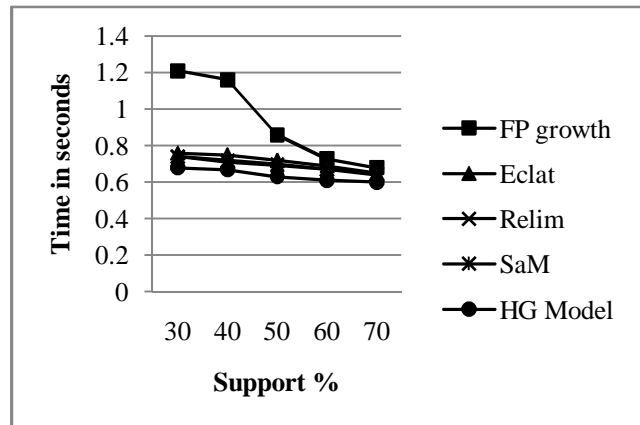


Figure 8 Performance analysis on Census data set

VII. CONCLUSION

In this paper a new data structure consisting of a hypergraph D is proposed for representing a TDB . Algorithms for constructing D , generating frequent patterns using D and for generating frequent subhypergraphs are presented. During the entire process the database is scanned exactly once. Several types of experiments to test the effect of changing the support, transaction size, dimension, transaction length and use of other hypergraph theoretic parameters are conducted to extract new knowledge about the TDB [9]. The comparison of the performance of this algorithm with other existing algorithms in the literature using real data set are also studied and analyzed.

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