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# Joint Non Linear and Distortion based PAPR Reduction Technique for Optical OFDM Systems

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**ABSTRACT:** Orthogonal Frequency Division Multiplexing (OFDM) has emerged as a promising modulation technique for high speed optical systems as it reduces intersymbol interference and offers high spectral efficiency. But it has an inherent drawback of high Peak to Average Power Ratio (PAPR) due to multiple subcarriers which makes it sensitive to non linear effects. Different techniques have been proposed for PAPR reduction in literature. This paper presents the joint modified sliding norm transform (SNT) combined with distortion based clipping technique for PAPR reduction in Optical OFDM systems. The CCDF shows improvement in PAPR using proposed methodology over existing modified SNT technique. The BER performance is considered to study the performance of the system.

**KEYWORDS**: Orthogonal Frequency Division Multiplexing (OFDM), Peak to Average Power Ratio (PAPR), Complementary Cumulative Distribution Function (CCDF), Clipping, Modified Sliding Norm Transform (SNT).

# I. INTRODUCTION

OFDM is a spectrally efficient multiple carrier modulation format which converts high data rate channel into multiple lower data rate channels which are spectrally orthogonal to each other. Some of the applications of OFDM include digital subscriber lines, high-definition television broadcasting, long-term evolution based cellular networks and long haul optical communication [1]. OFDM is considered as a suitable technique for high speed optical communication due its due its inborn favorable advantages of lessening in intersymbol interference and high spectral efficiency [2].However, the significant issue with OFDM is high PAPR value which emerges because of large number of subcarriers which increases the non linear effects and also puts a constraint on range of nonlinear network devices such as analog-to-digital converters, amplifiers and modulators. Hence there is a need to lessen the PAPR of OFDM signal in optical OFDM systems.

# II. RELATED WORK

In [1], the authors have given a review on the principles, advantages, challenges, and practical requirements of optical orthogonal frequency division multiplexing (OFDM)-based optical access. High PARP has emerged to be the main problem of OFDM system. In [3], authors present a simple and efficient clipping based PAPR reduction technique but it introduces clipping noise. To combat the problems of distortion, techniques like PTS and SLM have been presented in [4],[5] but they require large computations leading to low data rates. A non linear transform based SNT technique has been presented in [6] which does not require large computations.[7] presents modified SNT which uses two samples instead of three samples as used in [6] for PAPR reduction. In this paper modified SNT along with clipping technique has been used to reduce PAPR.

# III. OPTICAL OFDM SYSTEM

With OFDM modulation technique, the data stream to be transmitted is split into a number of parallel low data rate bit streams. The generation of OFDM signal can be realized using Inverse Fast Fourier Transform (IFFT). At the receiver, Fast Fourier Transform (FFT) is used to recover data from OFDM sequence [8]. At the transmitter, high rate digital data stream is split into N parallel streams which are mapped using some modulation scheme after which IFFT



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is performed to obtain OFDM signal.. After that, a cyclic prefix is added to the OFDM symbol by adding samples from end of the sequence to the start of the sequence to reduce the effects of inter carrier interference (ICI). The generated OFDM sequence is then modulates the optical carrier which in this case is intensity modulation using Mach Zehnder modulator to which one input is electric OFDM signal and other input is optical carrier generated from laser source. Then the modulated signal is transmitted over an optical fiber. Figure 1 depicts the basic block diagram of an optical OFDM communication system.



Fig. 1. Schematic of optical OFDM system

At the receiver, after detection using photodiodes, the electric domain data is then converted from analog to digital using an analog-to- digital converter (ADC). After removing the cyclic prefix, the Fast Fourier transform (FFT) is performed to demodulate the data which is transformed from time domain to frequency domain . Finally, data is detected by demapping and parallel to serial conversion.

# IV. PAPR

A high peak to average power ratio (PAPR) is one of the major shortcomings of the OFDM modulation which occurs due to presence of a large number of subcarriers which when added coherently produces a large PAPR [9]. Mathematically, PAPR of a signal x(t) can be defined as given by (2).

$$PAPR = \frac{\max\{|\mathbf{x}(t)|\}^2}{E(|\mathbf{x}(n)|^2)}$$
(1)

Complementary cumulative distribution function (CCDF) is generally used for illustration of PAPR which is defined as the probability that the PAPR of an OFDM frame exceeds a threshold value and is expressed as given below [4].  $(PAPR > PAPR_{O}) = 1 - (PAPR < PAPR_{O})$ 

$$APR > PAPR_{O} = 1 - (PAPR \le PAPR_{O})$$
$$= 1 - (1 - \exp(-PAPR_{O}))^{N}$$
(2)

The value of PAPR of OFDM signal increases with increase in number of subcarriers and high PAPR value enhances the non linear effects of the optical fiber. The effective refractive index of fiber can be expressed as

$$\mathbf{n}_{eff} = \mathbf{n}_1 + \mathbf{n}_1 \,\mathbf{P}/\,\mathbf{A}_{eff} \tag{3}$$

Where P is the input power and  $A_{eff}$  is the effective core area of the fiber. From equation (3), it is clear that, the non linearities in the fibre place a constraint on the maximum optical power that can be launched into the fibre [9].By reducing the value of the PAPR of an OFDM signal, the power level of the output signal after modulation can be kept low. High PAPR also requires a high dynamic range of linear power amplifier, Digital to Analog/ Analog to Digital converters for operation in linear region. Hence there is need of reduction in PAPR of OFDM signal.

# V. PAPR REDUCTION TECHNIQUES

In order to reduce the high PAPR value in optical OFDM systems, various techniques have been proposed in literature [10].Some of the important techniques are signal clipping, companding, SLM, PTS, non linear sliding norm transforms etc.



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### A. Signal Clipping

Amplitude clipping is a simple technique to reduce the PAPR of OFDM signal. A predefined value of the amplitude is used to limit the peak value of the input signal. Signal having values higher than this threshold value are clipped to the threshold value as follows.

$$f(x) = \{A \text{ when } x > A, \\ x \text{ when } 0 \le x < A \}$$
(3)

The main problem in this case is that the amplitude clipping introduces undesired clipping noise giving rise to inband and out of band distortion [3] [11].

### B. Companding based signal distortion

The companding technique is a pre-distortion process in which the amplitude of the small signal is enlarged while the large signal remains almost the same [12]. Using this method signal amplitude is re-distributed after transformation which results in reduced PAPR. Also, the gain of PAPR reduction and noise enhancement are increased as  $\mu$  is increased. Hence there is increase in noise due to companding for a constant value of signal-to-noise ratio. It is important to choose values of companding parameters to avoid significant noise [13].

### C. Selected mapping (SLM) for PAPR reduction

In selected mapping method, M independent data blocks  $S_m = [S_{m,0}, S_{m,1}, \dots, S_{m,N-1}]^T$ ,  $m = 1, 2, \dots, M$  represent the same information are obtained by multiplying the original sequence with M uncorrelated sequence  $P_m$ . These are then forwarded into IFFT operation simultaneously. And then the PAPR is calculated for each vector separately. The sequence with the smallest PAPR is selected for final transmission.

The receiver is required to have information about selected phase vector sequence and ensure that the vector sequence is received correctly [5]. This can degrade the spectral efficiency of the system.

### D. Partial transmit sequence(PTS)

In this method, the original OFDM sequence is divided into several sub-sequences and each sub-sequence is multiplied by different weights until an optimum value is chosen.



Fig.2. Block diagram of PTS technique for PAPR reduction

As seen from figure 2, data information  $\mathbf{X}$  is separated into V non-overlapping sub-blocks and each sub-block vectors has the same size *N*. Thus, for every sub-block, it contains N/V nonzero elements and set the remaining to zero. The sub-block vector is given by

$$\widehat{X} = \sum_{\nu=1}^{\nu} b_{\nu} X_{\nu}$$
<sup>(5)</sup>

Where  $b_v(v=1,2,...,V)$  is a weight factor used for phase rotation .The OFDM signal in time domain is obtained by applying IFFT operation on  $X_{v}$ . Then a suitable factor combination  $\mathbf{b} = [b_{1,2},...,b_v]$  has to be selected which makes the resulting PAPR achieve optimum value. The additional cost have to pay is the extra V-1 times IFFTs operation which also reduces the data rate [4].



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E. Sliding Norm Transform(SNT)

Another method to reduce PAPR is SNT. It uses three samples,  $x_{n-1}$ ,  $x_n$ ,  $x_{n+1}$ , and a controlling parameter,  $\alpha$ , in each sliding window to calculate the output samples [6][9].

$$y_{n} = \frac{x_{n}}{\sqrt{\alpha + x_{n-1}^{2} + x_{n}^{2} + x_{n+1}^{2}}}$$
(6)

At the receiver, Inverse Sliding norm transform is applied as given below.

$$\mathbf{x}_n = \left(\sqrt[3]{\mathbf{x}_n^3}\right) \cdot sign(y_n) \tag{7}$$

A modified sliding norm transform has been presented in [7] which SNT uses two parameters  $\alpha$  and b. and offers less computational complexity. The values of a and b can be adjusted to obtain desired PAPR reduction and power spectral density. The modified sliding norm transform is defined in (9).

$$y_n = \begin{cases} x_o, & n = 0\\ \frac{x_n}{\sqrt{a+b.|x_n|^2 + |x_{n-1}|^2}} & n = 1,2,3\dots N - 1 \end{cases}$$
(8)

For reception, the inverse of the transform is applied as given in (10).

$$x_{n} = \begin{cases} y_{o}, y_{n} \neq 0, n = 0\\ y_{n}, \sqrt{\frac{a + |x_{n-1}|^{2}}{1 - b \cdot |y_{n}|^{2}}}\\ 0 & y_{n} = 0 \end{cases}$$
(9)

The variation in CCDF due to change in parameters a and b is depicted in figure 3. From figure 3(a), it is evident that value of PAPR increases with increase in a. For a >1, the PAPR starts increasing than original OFDM signal, so a is kept between 0 to 1.



Figure 3. Effect on change in parameter a and b on CCDF of OFDM signal

Also, PAPR reduces considerably with increase in b as evident in figure 3(b). Hence the values of a and b need to be optimized for desired results.



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The main advantages of SNT are improvement in terms out-of-band distortion in the system and the method does not require any side information to be transmitted and hence there is no loss in data rates [7]. The comparison of PAPR reduction capabilities of various PAPR reduction techniques is given in figure 4.



Fig 4. Comparison of PAPR reduction using various techniques (in dB)

As it can be seen from the figure 4, Clipping offers high value of PAPR reduction but high clipping ratio leads to enhancement in noise.SLM and PTS have high computational complexity.

Hence, in this paper, a joint PAPR reduction technique using modified SNT and clipping with a low clipping ratio has been proposed. Figure 6 represents the optical OFDM with PAPR reduction technique

# VI. SIMULATION RESULTS

PAPR reduction analysis in Optical OFDM Systems with proposed PAPR reduction technique has been done by comparing the PAPR for OFDM transmitted signal after applying the proposed methodology and simple OFDM transmitted signal using the CCDF. The various parameters used in the system are given in table 1.

S.	Parameter	Value
No.		
1	Baseband modulation	QAM 4
2	Bit rate	10 Gbps
3	Sampling rate	40 Gbps
4	No. of OFDM	64
	subcarriers	
5	Fiber span	200 km
6.	Carrier frequency	193.1
		THz

Table 1. List of parameters Of Optical OFDM syste
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In Figure 5(a), CCDF of OFDM signal shows the PAPR reduction performance of the Joint modified SNT and clipping technique. It is evident that PAPR reduction using modified SNT at a=1,b=2 is around 2.5 dB at threshold probability of  $1 \times 10^{-2}$  and is further reduced by 1 dB using the proposed method with clipping threshold of 0.2. The BER of received signal is also studied. Then OFDM signal with reduced PAPR is sent through Optical system Figure 6(b) represents the graph of BER with variation in OSNR of received signal.



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Figure 5. a) CCDF showing PAPR reduction using joint technique; b) BER vs OSNR of received signal

As shown in figure 5(b), the BER value reduces considerably with increase in OSNR of received signal. The proposed method provides good range of BER of the received signal where BER of  $1.23 \times 10^{-3}$  for the fiber span of 200km is obtained using the technique.

#### VII. **CONCLUSION AND FUTURE WORK**

OFDM is a promising technique for very high speed communication systems as it offers spectral efficiency and reduces intersymbol interference. But OFDM has inherent drawback of high PAPR due to a large number of subcarriers .Various methods have been proposed for reduction of PAPR of OFDM signal. The simplest method is clipping but it introduces noise for large clipping ratio. PTS and SLM give good performance but require extra information for reception. Modified SNT do not need any side information but PAPR reduction needs to be enhanced. This paper presents a joint Modified SNT and clipping as PAPR reduction technique for optical OFDM systems. The results depict the enhancement in PAPR reduction by 1 dB. System exhibits good performance in terms of BER using PAPR reduction technique.

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