



Diagonalizable Algorithm for Cell Scheduling in Fixed Virtual Output Queued (VOQ) Packets Switches

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ABSTRACT: Explosive growth in internet is demanding very fast switching fabric in internet routers and switches. Packets need to be buffered at input or output or on both sides of crossbar switching fabric. Crossbar switches are used for switching because of no bandwidth limitation & high scalability. It's well known fact that buffering of packets on outside of switch demands switching fabric to be 'N' time faster whereas buffering packets on input side limits throughput to 58%. Combined input output queued (CIOQ) switch demands that switch fabric to run at speed up of 2. VOQ (Virtual output Queue) i.e. 'N' queues per input port i.e. total N^2 queues on input side are suggested to resolve problem of throughput limitation of 58%. In VOQ throughput achieved is 100%. Selection of packets is the key issue in VOQ, Various schemes like, Maximum Weight matching (MWM), Maximum Size Matching MSM and maximal matching, are suggested by researchers in last two decades to improve the performance in terms of throughput and delay. Because of constraint of selecting one cell from an input port and sending one cell to an output port in a time slot puts limitation that selected elements are only diagonal elements. Such permutation of diagonal are $N!$ Choosing appropriate diagonal is key issue in cell scheduling. We are addressing Diagonalizable Maximum Weight Matching (DMWM) Scheme which provides 100% instantaneous throughput in each slot under heavy traffic conditions & improves delay performance. Our scheme DMWM is computationally complex for large size switches but it outperforms at lower size switches and provides optimal performance nearer to output queued switch. We have also modified our DMWM to Modified DMWM (MDMWM) to reduce the computational complexity.

KEYWORDS: Fixed length packet switches, Maximum weight matching algorithms, Packet Scheduling, VOQ

I. INTRODUCTION

Internet services are growing faster and faster and it's becoming part of everybody's life. Demand for fast internet service is increasing pressure on router design engineers to provide faster switching architectures. Basically cross bar switches are used in internet router/switches because of scalability and no bandwidth limitation exist with it. Present switches use crossbar switches along with buffering of packets either on input- output or on combined input output. Output queued switches provides 100% throughput but requires N times faster switch fabric. Input queued switch does not required N times faster switch fabrics but suffered from throughput limitation to 58%. Virtual Output queued (VOQ) switch provides 100 % throughput without N time faster switch fabric but scheduling or selection of cell from N^2 queues is the key issue.

II. RELATED WORK

Virtual output queues (VOQ) in which packets are buffered or input side destined for each output separately [2], [3], and [5]. This demand for N^2 queues on input side. VOQ technique has resolved problem of throughput limitation of 58% where single input queue is used [1], [2], and [4]. VOQ suffers from scheduling of packets. There are total N^2 packets at HOL and we need to choose N non-conflicting packets delivered to the output to achieve throughput of 100% in each time slot.

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Packet scheduling schemes are suggested and they are generally classified as MaximumSize Matching, Maximum Weight Matching,Maximal Matching and Maximal Matchingwith iteration and Maximal Weight matchingwith and without iteration [1], [5].

Maximum size matching guarantees for instantaneous throughput to be 100% but donot guarantee for good delay performance.Maximum weight matching scheme gives thebest performance equivalent to output queuedswitch but they are very complex in implementation [1], [8], [9].

A maximum matching is largest size matching that can be made on graph whereasmaximal matching is matching to which no further edges can be added without first removing an already matched edge. Hence maximummatch can be maximal but vice versa is not true.

Maximal matching provides good through-put performance and poor delay performance.Iterative maximal matching and its variantsuch as i-slip; DRR, FIRM, SRA, etc. provide good throughput and delay performancein multiple iteration. Expected number of iterations are $O(\log(N))$. There are some variantssuch as weighted i-slip, i-LQF, i-OCF, etc. [1],[6], [7],[10]which gives good delay performancebetter than simple i-slip but these are complexto implement in hardware.

Recent researchers worked on to reduce communication overheads reduction in complexity of hardware, stability, scalability, fairness, etc. Still efforts are made by researchersto provide best optimal solution for scheduling policy in selection of packets in VOQ [1], [7], [8]. Our efforts are also to provide scheduling scheme named as Permuted Diagonal Maximum Weight Matching scheme to provide gooddelay and throughput.

III. VOQ SWITCH

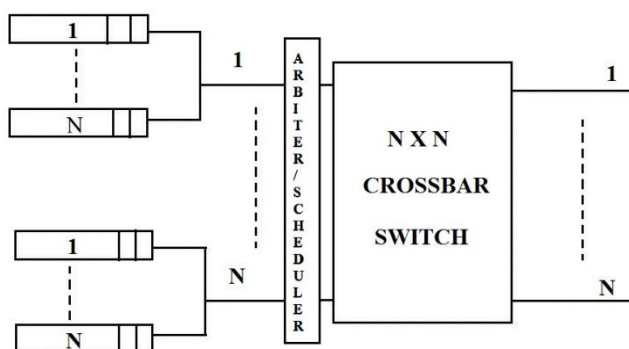


Fig. 1. VOQ switch model

Switch model is as shown in Fig. 1 is $N \times N$ switch with multiple input queues used to storethe arriving packets to input port 'i' and destined to output port 'j' in j^{th} queue at inputport i. Hence there are 'N' queues per inputport. There are total N^2 queues at input sideof switch. Time assumed to be slotted witheach slot equal to transmission time of a cell orpacket. In each cell slot we select at most 'N'packets from N^2 HOL packets. We have putconstraint that at most one HOL packet willbe chosen from each input port and at mostone packet will be delivered to an output port.Hence we constrain pattern I of $N \times N$ matrixsuch that Where, I_{ij} is permutation of indicator matrix. Indicator queue-length matrix K isformed such that $K_{ij}=1$ if Queue-length matrix $L_{ij} > 0$ else $K_{ij}=0$.

IV. PROBLEM DEFINITION

A scheduling problem in crossbar based VOQ switches can be resolved by finding optimal weight matrix using VOQ occupancies reported in Queue-length matrix L.

$L_{ij}(t)$ = Number of packets backlogged at time $(t-1) +$ arrival if any, at time $(t-1)$ to t -departure if any of HOL packet at end of time (t) ; where $1 \leq i, j \leq N$.

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It is basically constructing bipartite graph $G = (V, E)$ that consist of set V of $2N$ vertices partitioned into two sets namely 'N' inputs and 'N' outputs. The set of edges E has one edge connecting vertex i of input to vertex j of output for each $L_{ij}(t) > 0$. A matching M on G is any subset of E such that no two edges in M have common vertex. Matching guarantees that only one packet per input and output needs to be transferred [1], [6], [7]. A scheduling policy should work under constraint mentioned above with aiming of instantaneous throughput of 100% and set $M \subset E$ has maximum weight. Hence M must satisfy:

1. Number of edges matched should be 'N'. If no such set exist then select 'M' such that it has maximal matched edges. This condition pulls throughput towards maximum.
2. A match 'M' obtained should have instantaneous average Queue-length $>$ overall average Queue-length an must have variance minimum which is calculated w.r.t. overall average Queue-length (L). These conditions need to select appropriate permuted diagonals where queues are blowing with higher rate and should be brought under control.

V. CELL SELECTION POLICIES

Random selection: In this policy of selection no weights are assigned to queues. Select randomly any input and switch the cell from it. Do not allow this input port and destined port for which cell is switched in current or previous round. It may happen that selected input port has no HOL cell or is having queue occupancy very low. In such cases instantaneous throughput will be reduced and backlog will increase yield in poor delay performance. Generally it may or may not be optimal solution [1], [9].

Maximum Queue Length (MAXQ): It is a greedy policy where highest backlog input is identified and selected first. Here weight $W_{ij} = L_{ij}$, $1 \leq i, j \leq N$. Again restriction of not selecting the same input & output in remaining round remains the same [1], [9].

R C Sum minimum: In this policy of selection queue length Indicator matrix is considered. Queue length indicator matrix is formed as

$$K_{ij} = \begin{cases} 1 & \text{if } L_{ij} > 0 \\ 0 & \text{if } L_{ij} = 0 \text{ where } 0 \leq i, j \leq N \end{cases}$$

This will reduce the number of bits required to handle in hardware implementation. Now weight W_{ij} is evaluated

$$W_{ij} = \sum_m K_{i,m} + \sum_n K_{n,j}$$

where $0 \leq i, j \leq N; 1 \leq m, n \leq N$

Here queue whose weight is higher being selected first for switching. The queue elements from corresponding row and column of selected element will not participate in further round. Such 'N' round will take place for selecting 'N' elements

VI. DIAGONALIZABLE MAXIMUM WEIGHT MATCHING ALGORITHM (DMWMA)

The aim of Diagonalizable Maximum Weight Matching Algorithm (DMWMA) is to maximize the instantaneous throughput subject to stabilize the switch. Since the stability of switch is critical for bounding packet delays and buffer over flow. Maximizing the through-put is not equivalent to maximizing the stability region. Therefore, the focus of this policy is to maximize one subject to certain constraint on the other. However, DMWMA is computationally very complex algorithm. Presently it is not possible to evaluate determinant value for a matrix of greater than 16×16 . Later modified MDMWMA is proposed which is computationally less complex.

This scheduling policy uses queue lengths of each input queues to calculate the weight matrix. It is based on the fact that the packet to be selected from a certain input queue (IQ) for switching must not only have higher queue length but also the other packets switching along with it in the same time slot must have significant queue lengths. This is necessary condition in order to maximize throughput and keep average delay in acceptable limits.



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$$W = \begin{bmatrix} - & - & - & - \\ - & - & W_{2,3} & - \\ - & - & - & - \\ - & - & - & - \end{bmatrix}$$

Let W be the weight matrix for N^2 queues. Let $W_{2,3}$ is weight for cells at input port 2 and destined for output port 3. Evaluating weight at HoL position of (i,j) in W matrix using queue length matrix 'L', needsto consider queue lengths of HoL which are not in i th row and j th column. This is due to our constraint of only one cell must beswitched from i th row and j th column. If HoL cell (i,j) exists then positional weight of certainHoL should not depend only on queue occupancy of packets destined for particular output port or number of packets from that input portdestined for various output ports but also depend on occupancies of queues in other inputports.

L is a matrix of size $N * N$ with each element l_{ij} indicating queue length of packet to be switched from input port i to output port j . The weight matrix W is calculated in order totake decision about which cells to be switchedin one time slot . w_{ij} indicates element of matrix W i.e the weightage of HOL packet of theinput port i and going to output port j .

$W_{ij} = L_{ij} * f(L_{ij})$, where $f(L_{ij})$ is some weighted function of all l_{mn} elements except $m \neq i$ and $n \neq j$ for all $1 \leq m, n, i, j \leq N$. It is observed that if $l_{ij} = 0$ then $W_{ij} = 0$ i.e. weight assigned to queue of i th input port buffering cells destined for j th output port.

Let M^{ij} denotes minor of matrix L and m_{1c}^{ij} indicates first row and c th column elementof matrix M^{ij} . The equation to find the weightmatrix is given in (1).

$$w_{i,j} = l_{i,j} * (F^{(r)})(M^{ij}) \tag{Equ(3)}$$

In eq(1), $F^{(r)}(M^{ij})$ is a recursive function. Where, r indicates level of recursion and varies from 1 to $(N - 1)$. Let Q_r represents thenumber of columns in M^{ij} matrix at r th levelof recursion. The minor of M^{ij} is indicated by M^{1c} . Then the recursive function $F^{(r)}(M^{ij})$ isevaluated as shown in eq (2).

$$F^{(r)}(M^{ij}) = \left\{ \begin{array}{ll} M^{ij} & \text{if } Q_r = 1 \\ \sum_{c=1}^{Q_r} m_{1c}^{i,j} * F^{(r+1)}(M^{1c}) & \text{otherwise} \end{array} \right\} \tag{Equ(4)}$$

In order to illustrate this method consider the example given below: Here L is of size $N * N$ (i.e $4 * 4$). Therefore r runs from 1 to 3.

$$L = \begin{bmatrix} l_{11} & l_{12} & l_{13} & l_{14} \\ l_{21} & l_{22} & l_{23} & l_{24} \\ l_{31} & l_{32} & l_{33} & l_{34} \\ l_{41} & l_{42} & l_{43} & l_{44} \end{bmatrix}$$

Step 1: with $(r=1)$

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$$W_{11} = l_{11} * F^{(1)} \left\{ \begin{bmatrix} l_{22} & l_{23} & l_{24} \\ l_{32} & l_{33} & l_{34} \\ l_{42} & l_{43} & l_{44} \end{bmatrix} \right\} \pi r^2$$

Step 2: with (r=2)

$$F^{(1)} \left\{ \begin{bmatrix} l_{22} & l_{23} & l_{24} \\ l_{32} & l_{33} & l_{34} \\ l_{42} & l_{43} & l_{44} \end{bmatrix} \right\} = l_{22} * F^{(2)} \left\{ \begin{bmatrix} l_{33} & l_{34} \\ l_{43} & l_{44} \end{bmatrix} \right\} + l_{23} * F^{(2)} \left\{ \begin{bmatrix} l_{32} & l_{34} \\ l_{42} & l_{44} \end{bmatrix} \right\} + l_{24} * F^{(2)} \left\{ \begin{bmatrix} l_{32} & l_{33} \\ l_{42} & l_{43} \end{bmatrix} \right\}$$

Step 2: with (r=3)

$$F^{(2)} \left\{ \begin{bmatrix} l_{33} & l_{34} \\ l_{43} & l_{44} \end{bmatrix} \right\} = l_{33} * F^{(3)} \{ |l_{44}| \} + l_{34} * F^{(3)} \{ |l_{43}| \} = l_{33} * l_{44} + l_{34} * l_{43}$$

$$F^{(2)} \left\{ \begin{bmatrix} l_{32} & l_{34} \\ l_{42} & l_{44} \end{bmatrix} \right\} = l_{32} * F^{(3)} \{ |l_{44}| \} + l_{34} * F^{(3)} \{ |l_{42}| \} = l_{32} * l_{44} + l_{34} * l_{42}$$

$$F^{(2)} \left\{ \begin{bmatrix} l_{32} & l_{33} \\ l_{42} & l_{43} \end{bmatrix} \right\} = l_{32} * F^{(3)} \{ |l_{43}| \} + l_{33} * F^{(3)} \{ |l_{42}| \} = l_{32} * l_{43} + l_{33} * l_{42}$$

Step 4:

$$w_{11} = l_{11} * (l_{22} * (l_{33} * l_{44} + l_{34} * l_{43}) + l_{23} * (l_{32} * l_{44} + l_{34} * l_{42}) + l_{24} * (l_{32} * l_{43} + l_{33} * l_{42})) \quad \text{Equ(5)}$$

Similarly, calculate all the other elements of weight matrix W.

The calculation of weight matrix W fails when one or more rows/columns in the queue length matrix L are zero. i.e. if any input port is out of service or there is no packet going to certain output port. In order to solve this problem a matrix L' is formed given by

$$L' = L + U$$

Where, U is a square matrix of size N*N with all ones. The L' matrix is used instead of L matrix to calculate weight matrix W. Since, the L' matrix does not contain any zero element it gives correct weight matrix in any case. This is illustrated by an example EX-2.

After the weight matrix is calculated, the next step is to select the optimal diagonal for switching. This is done by first selecting the maximum weighted queue say W_{ij} . All the entries in weight matrix corresponding to the input port i and output port j are made invalid for selecting next element. Again an element having maximum weight among the remaining valid entries in the weight matrix is selected. This process continues until N input queues are selected for switching. Finally the DMWMA is summarized by following algorithm:

1. Get queue length matrix L.
2. Calculate L' matrix from L matrix by using $L' = L + U$.
3. Evaluate Weight Matrix W from L' matrix by using eq(3).
4. Select N optimal diagonal elements using weight matrix W as discussed above.



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5. Switch packets corresponding to selected N diagonal elements, if and only if a packet is present in the corresponding queue.
6. Go to step 1 and Repeat till there are no elements left for selection.

Complexity in DMWMA: In this algorithm number of multiplication required are (N-1).(N-1)! and additions (N-1)! - 1, which is very high. It's difficult to implement with present parallel hardware infrastructure available. But DMWMA truly finds the weight of queue. In this algorithm queue length of each queue contribute to weight of other queue approximately.

VII. MODIFIED DIAGONALIZABLE MAXIMUM WEIGHT MATCHING ALGORITHM(MODIFIED DMWMA)

The Modified Diagonalizable Maximum Weight Matching Algorithm (Modified DMWMA) is computationally less complex as compared to DMWMA. In order to maximize the throughput subject to minimize the delay, the selection of queue for switching the packet from it depends on:

- The queue length of that queue.
- The average queue length of the queues from which the packets can be switched along with packet from that queue (supportive queues).
- The average queue length of the queues from which the packets cannot be switched along with the packet from that queue (competitive queues).

Consider a 4*4 queue matrix.

$$L = \begin{bmatrix} l_{11} & l_{12} & l_{13} & l_{14} \\ l_{21} & \underline{l_{22}} & l_{23} & l_{24} \\ l_{31} & l_{32} & l_{33} & l_{34} \\ l_{41} & l_{42} & l_{43} & l_{44} \end{bmatrix}$$

Suppose, l_{22} is selected queue. Then the supportive queue elements are shown by underline in below matrix.

$$L = \begin{bmatrix} \underline{l_{11}} & l_{12} & \underline{l_{13}} & \underline{l_{14}} \\ l_{21} & \underline{l_{22}} & l_{23} & l_{24} \\ \underline{l_{31}} & l_{32} & \underline{l_{33}} & \underline{l_{34}} \\ \underline{l_{41}} & l_{42} & \underline{l_{43}} & \underline{l_{44}} \end{bmatrix}$$

The competitive queues of the queue l_{22} are underlined in the matrix shown below:

$$L = \begin{bmatrix} l_{11} & \underline{l_{12}} & l_{13} & l_{14} \\ \underline{l_{21}} & l_{22} & \underline{l_{23}} & \underline{l_{24}} \\ l_{31} & \underline{l_{32}} & l_{33} & l_{34} \\ l_{41} & \underline{l_{42}} & l_{43} & l_{44} \end{bmatrix}$$

L is a matrix of size N * N with each element l_{ij} indicating queue length of packet switching from input port i to output port j. Where $1 \leq i, j \leq N$. The weight matrix W with W_{ij} as element of W is calculated in order to take decision about which cells to be switched in current time slot.

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Consider, S_{avg} as average value of queue length of supportive queues at position ij . It is evaluated using eq (6). Let C_{avg} be average value of queue length of competitive queues at position ij . It is evaluated using eq (7). Then the weight matrix is evaluated using eq(6),eq(7),eq(8)

$$S_{avg}^{ij} = \left(\sum_{r=1}^N \sum_{c=1}^N l_{rc} \right) / (N-1)^2 \quad \text{Equ(6)}$$

for $r \neq i$ or $c \neq j$
Equ(7)

$$C_{avg}^{ij} = \left(\sum_{r=1}^N \sum_{c=1}^N l_{rc} \right) / (2 * (N-1))$$

for $r = i$ or $c = j$

$$W_{ij} = l_{ij} * s_{avg}^{ij} / c_{avg}^{ij} \quad \text{Equ(8)}$$

The modified DMWMA is an approximation of DMWMA. So it gives sub-optimal solution in some extreme cases as considered in EX-1.

VIII. EXAMPLES

EX-1

Consider a queue length matrix as shown below:

$$L = \begin{bmatrix} 0 & 1 & 2 & 3 \\ 4 & 5 & 6 & 7 \\ 8 & 9 & 10 & 11 \\ 12 & 13 & 14 & 15 \end{bmatrix}$$

Average queue-length of entire queue occupancy = $(0 + 1 + 2 + \dots + 16) / 16 = 7.5$

The weights of selected diagonal are underlined.

Random Selection: Applying Random selection will select the elements randomly as discussed earlier. The resultant matrix after applying Random selection policy:

$$L = \begin{bmatrix} \underline{0} & 1 & 2 & 3 \\ 4 & 5 & 6 & \underline{7} \\ 8 & \underline{9} & 10 & 11 \\ 12 & 13 & \underline{14} & 15 \end{bmatrix}$$

Maximum Queue length (MAXQ): Applying Maximum Queue length will select the longest queue-length element first and will repeat N times. N being 4 here. The resultant matrix after applying Maximum queue length policy:



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$$L = \begin{bmatrix} \underline{0} & 1 & 2 & 3 \\ 4 & \underline{5} & 6 & 7 \\ 8 & 9 & \underline{10} & 11 \\ 12 & 13 & 14 & \underline{15} \end{bmatrix}$$

Here the summary of result and calculation will be :

Number of cells switched = 3, average queue-length of diagonal selected for switching = $(15 + 10 + 5 + 0)/4 = 7.5$

Variance = $\{(15-7.5)^2 + (10-7.5)^2 + (5-7.5)^2 + (0-7.5)^2\}/4 = 31.25$

RC Sum policy: Weight matrix by using

RC sum policy:

$$W = \begin{bmatrix} \underline{6} & 7 & 7 & 7 \\ 7 & 8 & \underline{8} & 8 \\ 7 & \underline{8} & 8 & 8 \\ 7 & 8 & 8 & \underline{8} \end{bmatrix}$$

Here the summary of result and calculation will be :

Number of cells switched = 3, average queue-length of diagonal selected for switching = $(0 + 6 + 9 + 15)/4 = 7.5$

Variance = $\{(0-7.5)^2 + (6-7.5)^2 + (9-7.5)^2 + (15-7.5)^2\}/4 = 29.25$

Since some of the queue-length elements in weight matrix are having the same weight we can say that there can be many versions of weight matrix, after application of final step of RC Sum, i.e maximum weight selection, and one of which is going to get selected. But this is not feasible so we have to apply some logic at this point to select one of those possibilities. We have to go with random selection. It is observed that because of random selection no optimal solution can be obtained.

DMWMA: Weight matrix by using DMWMA:

$$W = \begin{bmatrix} 0 & 4352 & 7712 & \underline{10368} \\ 6512 & 6000 & \underline{5328} & 4592 \\ 7712 & \underline{6048} & 4800 & 3872 \\ \underline{8208} & 6032 & 4592 & 3600 \end{bmatrix}$$

Here the summary of result and calculation will be :

Number of cells switched = 4, average queue-length of diagonal selected for switching = $(3 + 6 + 9 + 12)/4 = 7.5$

Variance = $\{(3-7.5)^2 + (6-7.5)^2 + (9-7.5)^2 + (12-7.5)^2\}/4 = 11.25$

Modified DMWMA: Weight Matrix by using Modified DMWMA:

$$W = \begin{bmatrix} 0 & \underline{1.52} & 2.8 & 3.85 \\ 4.72 & 5.43 & \underline{6} & 6.44 \\ 6.77 & 7 & 7.14 & \underline{7.2} \\ \underline{7.2} & 7.12 & 7 & 6.81 \end{bmatrix}$$

Here the summary of result and calculation will be :

Number of cells switched = 4, average queue-length of diagonal selected for switching = $(1 + 6 + 11 + 12)/4 = 7.5$

Variance = $\{(1-7.5)^2 + (6-7.5)^2 + (11-7.5)^2 + (12-7.5)^2\}/4 = 19.25$

It is observed that though the solution is non-optimal, it is unique and near to optimal.

Also this modified DMWMA has less computational complexity which is a plus point for this kind of near optimal solution.

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EX-2

Consider a queue length matrix L as shown below

Average queue-length of entire queue occupancy = $(5 + 6 + 12 + 7 + 20 + 8 + 0 + 10 + 0)/9 = 7.56$

Random Selection: Applying Random selection will select the elements randomly as discussed earlier. The resultant matrix after applying Random selection policy:	Maximum Queue length (MAXQ): Applying Maximum Queue length will select the longest queue-length element first and will repeat N times. N being 3 here. The resultant matrix after applying Maximum queue length policy:	RC Sum policy: In RC Sum policy, first the indicator matrix is formed. Weight is calculated by taking sum of row and column elements of indicator matrix. No unique solution is possible as many places same weight is observed.
$W = L = \begin{bmatrix} \underline{5} & 6 & 12 \\ 7 & \underline{20} & \underline{8} \\ 0 & \underline{10} & 0 \end{bmatrix}$	$W = \begin{bmatrix} \underline{5} & 6 & \underline{12} \\ 7 & \underline{20} & 8 \\ \underline{0} & 10 & 0 \end{bmatrix}$	$W = \begin{bmatrix} \underline{5} & \underline{6} & \underline{5} \\ 5 & 6 & \underline{5} \\ \underline{3} & 4 & \underline{3} \end{bmatrix}$
Number of cells switched = Random	Number of cells switched = 2	Number of cells switched = 2
average queue-length of diagonal selected for switching = Random	average queue-length of diagonal selected for switching = 10.67	average queue-length of diagonal selected for switching = 4.67
Variance = Random	Variance = 77.21	Variance = 19.93

DMWMA: Weight matrix by using DMWMA:	MDMWMA: Weight matrix by using Modified DMWMA:
$W = \begin{bmatrix} 400 & 0 & \underline{840} \\ \underline{840} & 0 & 400 \\ 0 & \underline{1240} & 0 \end{bmatrix}$	$W = \begin{bmatrix} \underline{6.55} & 1.76 & \underline{19.3} \\ \underline{5.29} & 9.7 & 3.9 \\ 0 & \underline{10.66} & 0 \end{bmatrix}$
Number of cells switched = 3	Number of cells switched = 3
average queue-length of diagonal selected for switching = 9.67	average queue-length of diagonal selected for switching = 9.67
Variance = 8.66	Variance = 8.66

It is observed that though the solution is non-optimal, it is unique and near to optimal.

Also this modified DMWMA has less computational complexity which is a plus point for this kind of near optimal solution. Arrange queue length of selected packet is lower but its variance is smaller than other packet switching policies.

Special case: But, now here if consider a matrix having entire row or column zero i.e. if no cells are arrived to input port or no cells are destined to output port from any input port.

$$L = \begin{bmatrix} 5 & 6 & 12 \\ 7 & 20 & 8 \\ 0 & 0 & 0 \end{bmatrix}$$

Queue Length matrix Special Case

$$W = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Weight Matrix by using DMWMA

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Here, weight matrix is a Null matrix,so no decision can be taken for switching cells from queue. This problem can be solved by modifying the queue length matrix L to L' matrix as per $L' = L + U$.

$$L' = \begin{bmatrix} 6 & 7 & 13 \\ 8 & 21 & 9 \\ 1 & 1 & 1 \end{bmatrix}$$

Modified Queue Length matrix Special Case

$$W = \begin{bmatrix} 180 & 119 & 377 \\ 160 & 399 & 117 \\ 336 & 158 & 182 \end{bmatrix}$$

Weight Matrix by using DMWMA on L'

The actual switching is done by using L Queue length matrix .Hence if a queue containing zero packets is selected then no switching of packets is done from that queue.

The L' matrix of the matrix in EX-2i.e. (10) is given as

$$L' = \begin{bmatrix} 6 & 7 & 13 \\ 8 & 21 & 9 \\ 1 & 1 & 1 \end{bmatrix}$$

Modified Queue Length matrix Special Case

$$W = \begin{bmatrix} 720 & 119 & 1417 \\ 1200 & 399 & 657 \\ 336 & 1738 & 182 \end{bmatrix}$$

Weight matrix by using MDMWMA on L'

Here it is observed that the switching diagonal found by L and L' matrix is same. In general L' matrix can be used to calculate weight matrix in modified DMWMA instead of L.

IX. STATISTICAL ANALYSIS

\bar{L} = overall average queue-length of L

$$= \left(\sum_{i,j} L_{ij} \right) / N$$

\bar{D} = average queue length of selected permuted diagonal

$$= \left(\sum_{k=0}^{N-1} L_{(1+c),(c+k) \bmod N} \right) / N$$

Where: c= column of selected diagonalelements in 1st row

Var(D) = variance of diagonal element wrt. \bar{L}

$$= \left(\sum_{k=0}^{N-1} L_{(1+c),(c+k) \bmod N} - \bar{L} \right)^2 / N$$

T_n = Throughput at nth time slot = (number of cells switched * 100) / N

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Table 1. Result analysis of EX-1

Policy	\bar{L}	\bar{D}	Var (D)	T_n
RANDOM				75%
MAX QLength	7.5	7.5	31.25	75%
RCSUM MAX	7.5	7.5	29.25	75%
DMWMA	7.5	7.5	11.25	100%
MDMWMA	7.5	7.5	19.25	100%

Table 2. Result analysis of EX-2

Policy	\bar{L}	\bar{D}	Var (D)	T_n
RANDOM				100%
MAX QLength	7.56	7.5	31.25	66.67%
RCSUM MAX	7.56	4.67	19.93	66.67%
DMWMA	7.56	9.67	8.33	100%
MDMWMA	7.56	9.67	8.33	100%

Remark:DMWMA is best suitable algorithm because cell selected from diagonal elements has minimum variance and gives 100% instantaneous throughput. But computational complexity is very high. MDMWMA is near optimal solution. MDMWMA algorithm also gives 100% with instantaneous throughput but variance is higher than DMWMA. MDMWMA algorithm has computational complexity very less. It is observed in both example mentioned above. Following section represents the results obtained through simulation.

X. SIMULATION RESULT

A simulation is carried out with switch size of 8x8 with VOQ. Simulation is run for 10,000 slot time. Policies applied are random selection (RANDOM); Maximum queue length (MAXQ); RCSUM-MAX; DMWMA; and Modified DMWMA. While drawing the graphs of delay performance and throughput, all policies are taken into account and mentioned in Fig. 2, 3, 4 Fig. 5 & 6 compares performance of MAXqlength and MDMWMA.

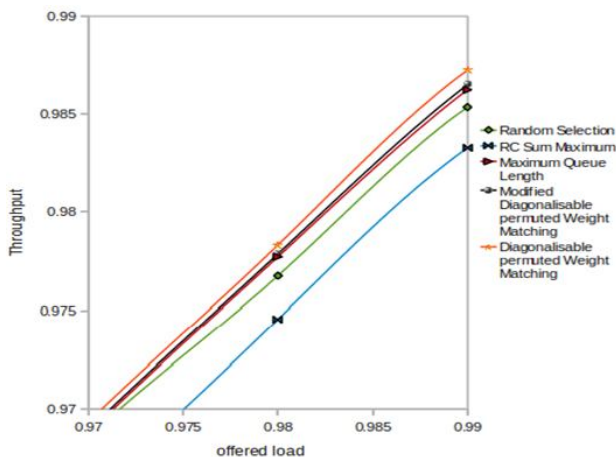


Fig. 2. Comparative analysis of throughput for 8x8 switch size with Bernoulli's traffic

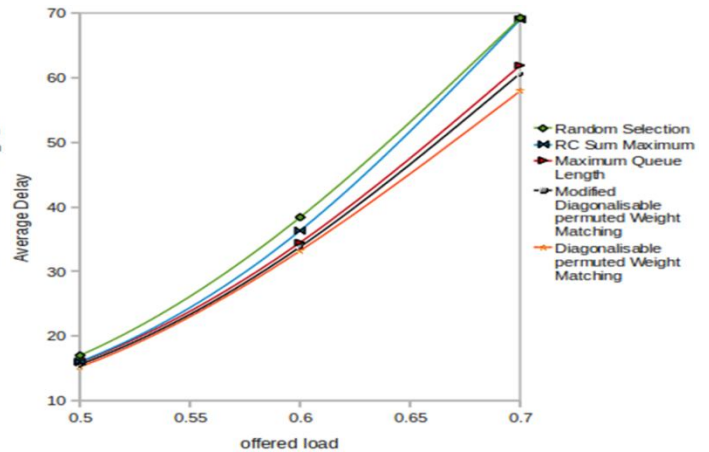


Fig. 3. Comparative analysis of delay time for 8x8 switch size with Bernoulli's traffic

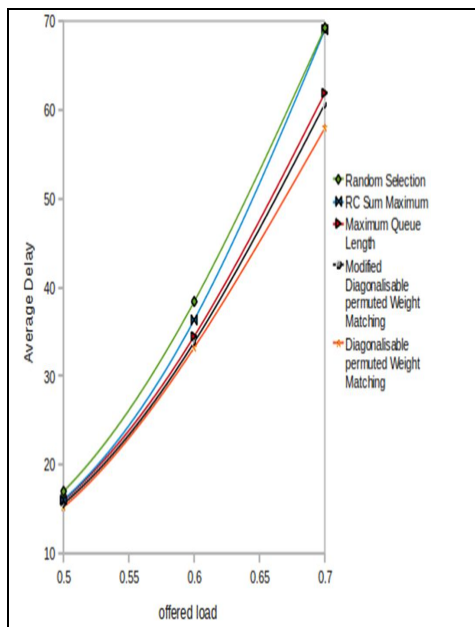


Fig. 4. Comparative analysis of avg. delay for 8x8 switch with bursty arrival traffic of burst size = 16

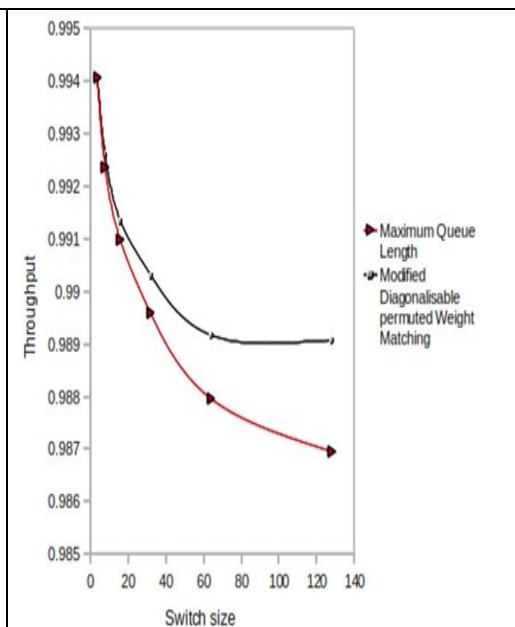


Fig. 5. comparative analysis of throughput Vs switch size for Bernoulli's arrival

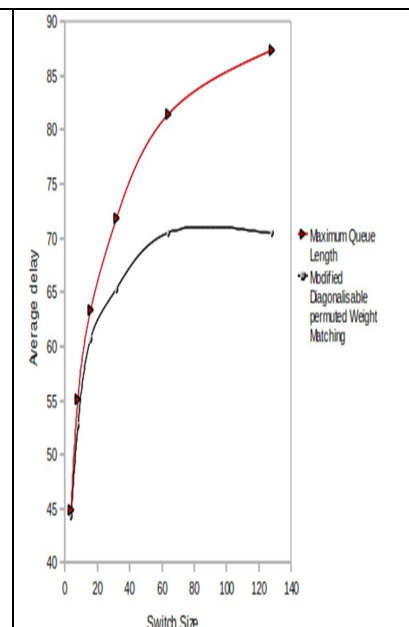


Fig. 6. Comparative analysis of delay time Vs switch size for Bernoulli's traffic

XI. CONCLUSION

DMWMA is providing unique and optimal solution for packet selection in VOQ switches. It's computationally complex but gives optimal solution. This is tested for various random queue occupancy matrix and observed that it improves the throughput delay performance. This is a theoretical attempt to show and suggest one method of MWM algorithm. We have modified DMWMA so that it can be implemented using parallel hardware architecture and gives near suboptimal solution. Above policies are stable policies.

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