



Using Wavelet Features for Analyzing Gamma Lines

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ABSTRACT: Data processing methods for analyzing gamma ray spectra with symmetric bell-shaped peaks form are considered. In many cases the peak form is symmetrical bell shaped in particular a Gaussian case is the most often used due to many physical reasons. The problem is how to evaluate parameters of such peaks, i.e. their positions, amplitudes and also their half-widths, that is for a single peak and overlapped peaks. Through wavelet features by using Marr wavelet (Mexican Hat) as a correlation method, it could be to estimate the optimal wavelet parameters and to locate peaks in the spectrum. The performance of the proposed method and others shows a better quality of wavelet transform method.

KEYWORDS: Gamma lines, Wavelet transform, Gamma Wavelet Transform Features.

I. INTRODUCTION

Gamma-ray spectroscopy around the middle of the last century focused largely on γ -rays emitted by radio nuclides produced in neutron, proton and α -induced reactions, using nuclear reactors and particle accelerators.

In parallel with the fast development of High Pure Germanium (HPGe) detectors of high resolution and usage of increased efficiency, the quality of gamma spectral analysis have increased. Of course, the analysis can be done graphically with good results but the need for numerical analysis is still in need especially when there are a large number of peaks to be located in a spectrum, or when many spectra are to be analyzed. This technique would not only provide saving in time but could also lead to even every small peaks could be easily detected [1].

Several methods have been reported for the computer analysis of gamma spectrum such as GAMANAL developed by Gunnink and Niday [2], HYPERMET developed by Philips and Marlow [3], and SAMPO developed by Rouiti and Prussin [4, 5].

The gamma spectrum of a source usually consists of discrete lines of very small width. Ideally a full-energy peak can be represented quite accurately by a one dimension Gaussian function:

$$f(x) = A \cdot \exp\left(-\frac{(x - x_0)^2}{2\sigma^2}\right), \quad (1)$$

where A is the maximum amplitude, x_0 is the centroid, and σ is the half-width. In such a doublet of two overlapping peaks can approximated as:

$$f(x; A, x_1; B, x_2) = A \cdot \exp\left(-\frac{(x - x_1)^2}{2\sigma_1^2}\right) + B \cdot \exp\left(-\frac{(x - x_2)^2}{2\sigma_2^2}\right), \quad (2)$$

where x_1, x_2 are the center coordinates and σ_1, σ_2 are the half-widths

In the process of registration, a peak is to be discredited as a histogram $\{h_k\}$ on the interval $(x_{\text{beg}}, x_{\text{end}})$,

$$h_k = \frac{1}{\tau} \int_{x_{k-1}}^{x_k} F(x; A, x_1; B, x_2) dx, \quad (3)$$

where $x_k = x_{\text{beg}} + k\tau$, and τ is the bin width.

Before peaks are fitted, one must determine the peak-location and define the ranges of the channel to be used in the fitting of each group of peaks. Several methods have been developed for peak search. The sensitivity of any method can be varied to find more or fewer peaks that are statistical fluctuations, or structure in the spectral background, rather

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than real peaks. There are many methods of locating peaks in the spectrum, the most important one is the wavelet transformation which we are used it as a correlation method for peak searches. In the present work, we present a new and accurate method for peak location allows detecting all single and multiple peaks. The searching method depends on wavelet transform technique to locate all peaks. A wavelet function is scanned across the spectrum and over the width of the search function, each spectrum count is multiplied by the corresponding value of the search function then any channels in the correlation spectrum which are greater than zero represent channels within a peak.

II. GAUSSIAN WAVELET ALGORITHM

A wavelet transform involves the decomposition of a signal $f(x)$ at different scales and positions. In a WT treatment, all basis functions are $\Psi_{a,b}(x)$ derived from a mother wavelet $\Psi(x)$ through the following dilation and translation processes [6]:

$$\Psi_{a,b}(x) = a^{-1/2} \Psi\left(\frac{x-b}{a}\right) \quad a, b \in \mathbb{R}, a \neq 0, \quad (4)$$

where a and b are, respectively, the scale and position parameters, with $a > 0$ and b having arbitrary values. The continuous wavelet transform of $f(x)$ is given by:

$$W_{\Psi}(a,b)f = \frac{1}{\sqrt{C_{\Psi}}} \int_{-\infty}^{\infty} \Psi_{a,b}(x) f(x) dx, \quad (5)$$

where C_{Ψ} is the normalization constant [7]. In practical computation, since the spectrum to be analyzed is often discrete sampling data, the discrete form of Eq. (4) is necessarily used, which can be expressed as:

$$W_{\Psi}(a,b)f = \frac{1}{N} \frac{1}{\sqrt{|a|}} \sum_{k=1}^N \frac{1}{\sqrt{C_{\Psi}}} \Psi\left(\frac{x-b}{a}\right) f(x) \quad (6)$$

The formula (6) does not contain integral and this fact allows one to apply WT method for analyzing spectrum.

According to the Gaussian-like shape of our signals, it is natural to choose the family of vanishing momentum wavelets, since they are generated by a Gaussian distribution function.

WT method has been incorporated into a computer code which called Gamma Wavelet Transform Model (GWTM). The program performs peak search for single and multiple peaks, fitting peaks, and line shape calibrations. The code has been used with a variety of spectra detected by HPGe detectors

The peak search method is based on using wavelet function to scan whole spectrum. This is demonstrated in Figure 1.

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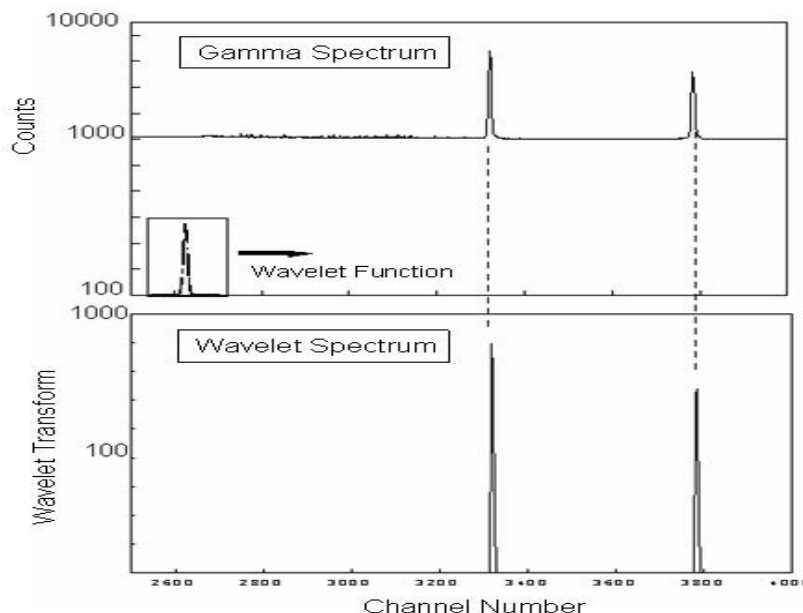
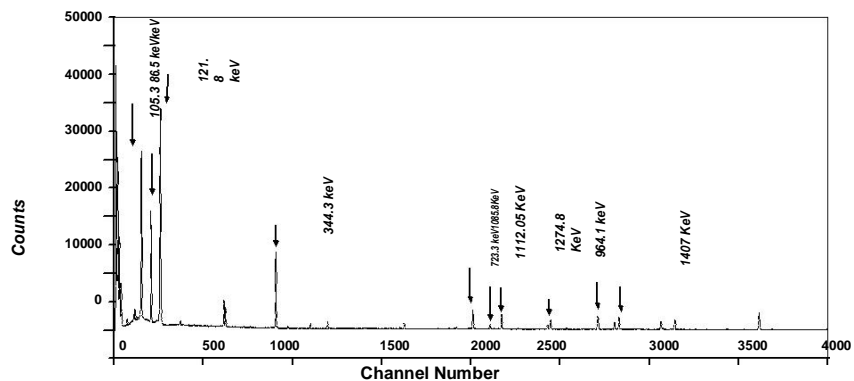


Figure 1: Wavelet function scans the whole gamma spectrum.

The program starts by reading gamma spectra. The original data from the multichannel analyzer or analyzer build in a computer system are saved in ASCII input data file with 4096 or more rows. After reading input file, GWTM goes to the calibration step. WT function reads the input data file to locate all peaks along the whole spectrum with subtraction from the background. Every point in the wavelet spectrum represents a peak with known centroid. GWTM program produces one output file. It contains the whole analysis of the spectrum. A sample output file is shown in Table 1. The performance of the method and the computer program were tested by analysis of gamma spectra of some radioactive isotopes, which are detected by a vertical HPGe detector surrounded by a lead shield with resolution 2.3 keV at 1332.5 keV. These Spectra are $^{152,154,155}\text{Eu}$, ^{133}Ba , and ^{60}Co as shown in Figures 2, 3, 4. Comparison between GWTM and a graphical method by PCAIII program is summarized in Tables 2, 3, 4.



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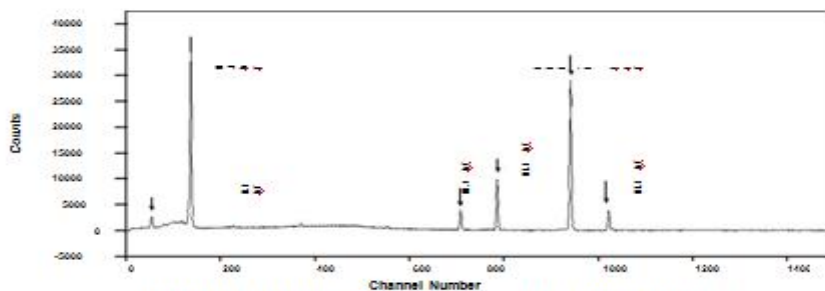


Figure 3: 133Ba spectrum detected by HPGe detector

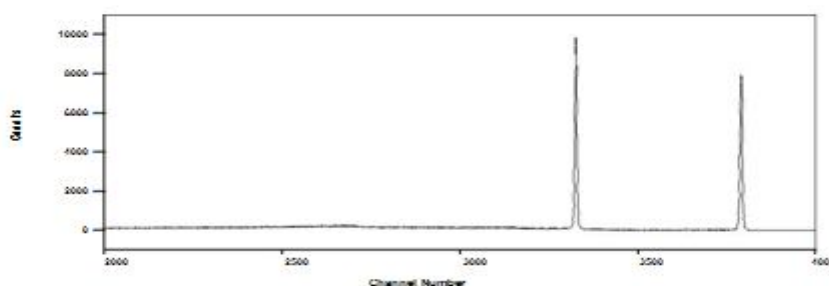


Figure 4: 60Co spectrum detected by HPGe detector.

Table 1: A sample run of GWTM code.

```

Number of Peaks= 6
-----
PN   PeakEnergy  FWHM_keV  Net_Area
-----
  1   3325.312  1173.482  3.2928  72089.3
  2   3323.025  1172.698  1.7836  67778.05
  3   3322.332  1172.46   2.744   70899.4
  4   3787.851  1332.133  2.8812  65435
  5   3787.614  1332.052  2.744   65078
  6   3787.659  1332.067  2.4696  64640.65
-----
InputFile: f:\samples\co60.txt
OutputFile:f:\samples\co60.wgm
-----
Energy Calibration equation is E(ch)= 32.9+0.343*ch
The Minimum detectable Resolution= 10
The Minimum Limit for peak area detected= 2000
-----
*****
*   YOUR PROGRAM FINISHED SUCCEFFULLY   *
*****

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Table 2: Comparison of GWTM and PCAIII for analysis of ^{60}Co spectrum

| E_γ (keV) | Centriod Peak (channel) | | | Net Area 10^4 (counts) | | |
|---------------------|----------------------------|---------|---------|-----------------------------|--------|---------|
| | GWTM | PCAIII | Diff(%) | GWTM | PCAIII | Diff(%) |
| 1173.2 | 3323.65 | 3323.06 | 0.0058 | 7.025 | 7.108 | -8.3 |
| 1332.5 | 3787.54 | 3787.46 | 0.0008 | 6.5051 | 6.5497 | -4.46 |

Table 3: Comparison of GWTM and PCAIII for analysis of $^{152,154,155}\text{Eu}$ spectrums

| E_γ (keV) | Centriod Peak (channel) | | | Net Area 10^4 (counts) | | |
|---------------------|----------------------------|----------|---------|-----------------------------|---------|---------|
| | GWTM | PCAIII | Diff(%) | GWTM | PCAIII | Diff(%) |
| 86.5 | 158.8 | 158.7719 | 0.0008 | 11.8263 | 11.7418 | 8.45 |
| 105.3 | 212.2 | 212.29 | -0.0009 | 9.538 | 9.5631 | -2.51 |
| 121.8 | 258.84 | 258.8304 | 9.5E-05 | 2.73037 | 2.8578 | -12.74 |
| 123.1 | 265.48 | 265.4678 | 0.0002 | 10.19649 | 10.3179 | -12.14 |
| 344.3 | 911.37 | 911.345 | 0.0002 | 6.9121 | 6.8396 | 7.25 |
| 723.3 | 2017.62 | 2017.37 | -5.204 | 2.10912 | 2.2373 | -12.81 |
| 904 | 2536.2 | 2535.67 | 0.0053 | 0.05782 | 0.0336 | 2.42 |
| 964.1 | 2717.1 | 2716.95 | 0.0015 | 1.15682 | 1.0186 | 13.82 |
| 1004.7 | 2837.78 | 2837.71 | 0.0007 | 1.484405 | 1.5064 | -2.19 |
| 1274.4 | 3622.32 | 3622.34 | -0.0002 | 1.41284 | 1.3757 | 3.71 |
| 1408 | 4039.64 | 4039.59 | 0.0005 | 1.7513 | 1.8317 | -8.04 |

Table 4: Comparison of GWTM and PCAIII for analysis of ^{133}Ba spectrum

| E_γ (keV) | Centriod Peak (channel) | | | Net Area 10^4 (counts) | | |
|---------------------|----------------------------|---------|----------|-----------------------------|---------|---------|
| | GWTM | PCAIII | Diff(%) | GWTM | PCAIII | Diff(%) |
| 53.2 | 59.48 | 59.47 | 4.7E-05 | 0.926 | 0.8531 | 7.29 |
| 81.2 | 136.12 | 135.91 | 0.00201 | 14.922 | 14.9776 | -5.56 |
| 276.4 | 707.6 | 707.60 | -9.3E-05 | 1.719 | 1.8065 | -8.75 |
| 302.8 | 786.46 | 786.44 | 0.00016 | 4.343 | 4.3237 | 1.93 |
| 356.2 | 939.56 | 940.52 | -0.0067 | 13.285 | 13.3143 | -2.93 |
| 383.9 | 1021.48 | 1020.99 | 0.00488 | 1.969 | 2.0787 | -10.97 |

IV. CONCLUSION

To summarize, wavelet transform is used to extract the spectral information efficiently from gamma spectra. In this method, estimation of peak number, peak position and half-widths can be determinate with high efficiency. The method has been incorporated into a general – purpose C++ computer program. The code has been used with different spectra detected by HPGe detector. The performance is evaluated with test cases and by comparing the results of $^{152,154,155}\text{Eu}$, ^{133}Ba , and ^{60}Co spectra which shows a good agreement.

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