

# Effect of Length on Correlation of PN Sequence and Gold Sequence

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**ABSTRACT:** Spread spectrum modulation technique is different from the conventional communication system. A good correlation property and large linear period of Pseudo-random sequence is the basis of spread spectrum communication systems intern CDMA (code division multiple access communication systems). Out of several techniques to implement direct sequence spread Spectrum (DSSS), one technique PN (pseudo noise) sequence/ code which is referred as the high rate digital code is generated on MATLAB. This generated m-sequence is then converted into polar format. Finally, in this paper we examine autocorrelation of PN sequence, GOLD sequence and compares the simulated autocorrelation with theoretical measured autocorrelation function at different value of N.

**KEYWORDS:** Autocorrelation-sequence, MATLAB, PN sequence, Spread spectrum communication, Pseudo-noise.

## I. INTRODUCTION

Spread Spectrum is a method of transmission in which the data sequence occupies a bandwidth in excess of the minimum bandwidth necessary to send it [1]. Spread spectrum techniques are used in many military communication systems to provide some combination of ranging capabilities, anti-jam protection, low probability of detection and interception, and multiple-access capability [4]. The spread spectrum communication has many advantages like strong anti-interference ability, low bit error rate, good hiding, low intercept, high confidentiality, etc [2].

Spread spectrum communication has two characteristics first one is the bandwidth of the signal transmission is much larger than the bandwidth of the original information signal and the second is that the transmission signal bandwidth is decided by the spreading codes (and the spreading codes are usually the pseudo-random code) [1]. There are several techniques by which spread spectrum can be implemented. One technique is called direct-sequence and the other technique is a PN (pseudo-noise) code which exhibits random-like properties which are necessary for providing good spectral characteristics and security [5]. A long PN code is frequently used for uplink channelization in the CDMA mobile communications [3]. Pseudo-random sequences with good correlation property, large linear complexity, and balance statistics are widely used in modern communication [6].

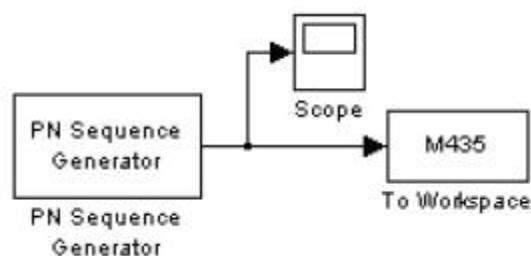


Figure 1. M sequence generation circuit simulation model[3]

Spread spectrum data transmission system using orthogonal codes has some difficulties mainly its autocorrelation property is often poor so a new method by which data are modulated onto PN codes generated from PN generators having the same feedback logic and different initial phases are generally used [7]

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In a Direct Sequence Spread Spectrum (DSSS) system, random binary data having bit rate of  $r_b$  bits per sec is Exclusive Ored by a pseudorandom binary waveform, which is at much higher rate and it provides the frequency spreading operation. This pseudorandom binary source outputs symbols called chips at a constant chip rate  $r_c$  chips per sec. Each bit in the pseudorandom binary sequence is known as a chip and the inverse of its period as chip rate. The chip rate is always higher than the bit rate, and the ratio of the chip rate to the bit rate is known as the processing gain [8]

M sequence is commonly used pseudo-random sequence, which is the longest linear sequence shift register. Such sequence has good autocorrelation characteristics. Shift register sequence is a periodic sequence, its cycle not only relate to the degree of the shift register, but also relate to the linear feedback logic and shift register initial state[1].

PN Sequence Generator generates a sequence of pseudorandom binary numbers by using shift register, as shown in Figure 2. There are  $r$  registers in the generator which update their values at each time step depending on the value of the incoming arrow to the shift register. The shift register is described by the Generator Polynomial parameter, which is a primitive binary polynomial in  $z$ ,  $g_r z^r + g_{r-1} z^{r-1} + \dots + g_0$ . The coefficient  $g_i$  is 1 if there is a connection from the  $i$ th register. The leading term  $g_r$  and the constant term  $g_0$  of the Generator Polynomial parameter must be 1.

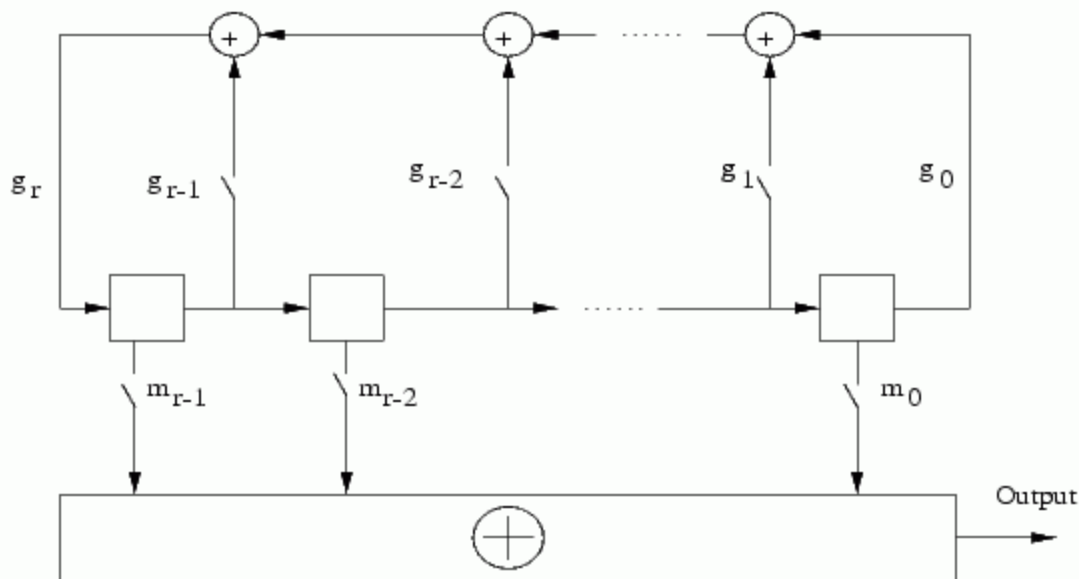


Figure 2. M-Sequence Generator Structure [2]

The adders perform addition modulo 2. The period of a PN sequence produced by a linear feedback shift register with  $m$  flip flops cannot exceed  $2^m - 1$ . When the period is exactly  $2^m - 1$ , the PN sequence is called a maximal length sequence or m-sequence. The remainder of this paper is organized as follows: Section 2 presents the material and method of the designed system for generation of m sequence and its autocorrelation in MATLAB. Section 3 gives a detailed discussion on the results obtained. The final section concludes and describes the future scope of this work.

## II. MATERIAL AND METHOD

To generate PN sequence MATLAB v 7.0 is used. A PN sequence is generated by means of a feedback shift register. PN sequence generated is determined by the length  $m$  of the shift register, its initial state and the feedback logic. The procedure followed in this work is detailed below. Firstly, NRZ encoder is used to get encoding data streams. There are three methods of encoding: Manchester, unipolar & polar. In this paper, Polar method is used. This data stream is used to generate m-sequence & then to find autocorrelation. Next step is to define the polynomial & m-

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sequence is generated. Then find autocorrelation of m-sequence by simulation. Autocorrelation also be calculated theoretically.

Method to calculate autocorrelation theoretically is Period of an m-sequence is defined by

$$N = 2^m - 1$$

m- Length of the shift registers.

Let  $c(t)$  is the resulting waveform of the maximum length sequence. Period of the waveform  $c(t)$  is

$$T_b = N \cdot T_c$$

$T_c$  is the duration assigned to symbol 1 or 0 in the maximal-length sequence.

Autocorrelation function of a periodic signal  $c(t)$  of period  $T_b$  is

$$R_c(\tau) = \frac{1}{T_b} \int_{-T_b/2}^{T_b/2} C(t) \cdot C(t - \tau) dt$$

Where the lag  $\tau$  lies in the interval  $(-T_b/2, T_b/2)$ . Using this formula autocorrelation is represented as

$$R_c(\tau) = \begin{cases} 1 - \frac{N+1}{N} |\tau|, & |\tau| \leq T_c \\ -\frac{1}{N}, & \text{for remainder period} \end{cases}$$

This theoretically autocorrelation is then compared with simulated Autocorrelation.

### III. RESULTS AND DISCUSSIONS

The resultant PN sequence (m-sequence) & polar format of that generated PN sequence is shown in Figure 2. This figure shows that number of binary 0s are differ by number of 1s by one chip only, which is the property of m-sequence. In first part of the figure, generated m-sequence is shown with respect to chip index and second part of the figure shows when this generated m-sequence is coded in polar format. In polar format, output is shown with respect to time.

Figure 4 & 5 shows the comparison of autocorrelation function of m-sequence simulated values with measured values of autocorrelation function for different values of lag  $\tau$ . These autocorrelation plots shows the number of agreements minus disagreements for the overall length of the two sequence (one is generated m-sequence and other is its time shifted sequence)

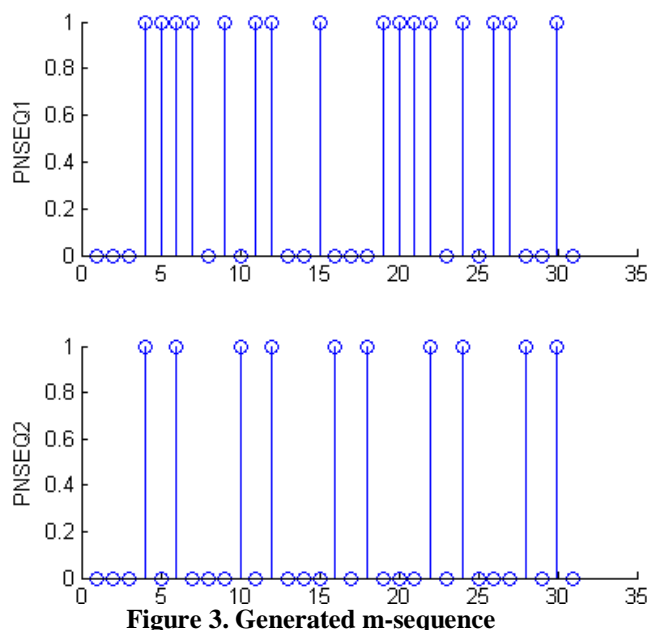


Figure 3. Generated m-sequence

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Figure 4 shows autocorrelation function when the polynomial is  $x^5+x^2+1$ . This figure shows that autocorrelation function increases or decreases linearly with the lag, so autocorrelation function is triangular. Figure 5 shows autocorrelation function when the polynomial is  $x^6+x+1$ . This figure shows that when the degree of polynomial increases autocorrelation function gives spike values.

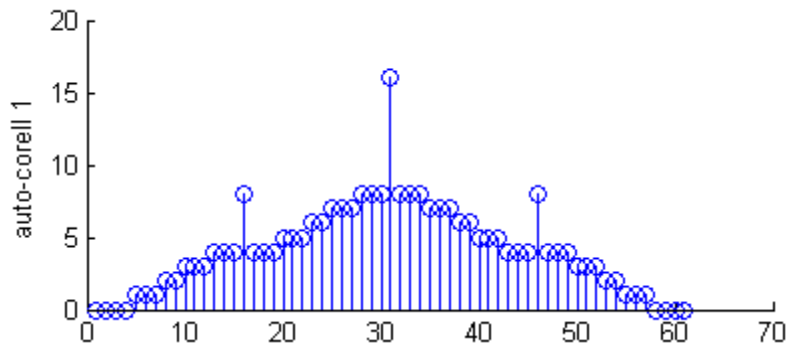


Figure 4. Comparison of theoretical & simulation values of autocorrelation for N=5

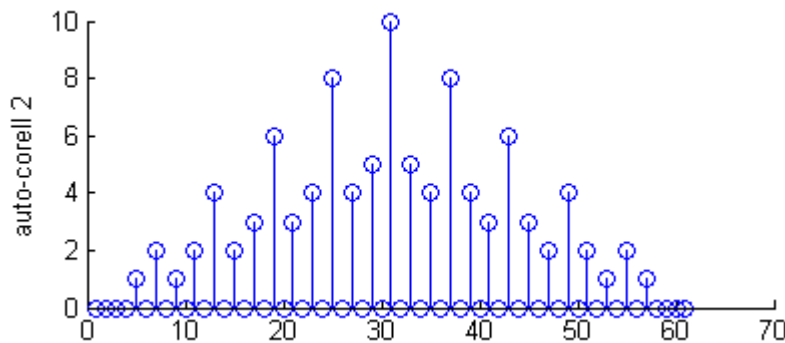


Figure 5. Comparison of theoretical & simulation values of autocorrelation for N=6

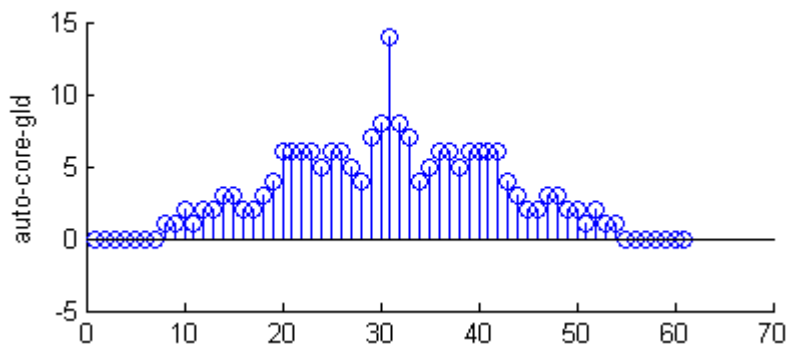


Figure 6. Cross correlation of gold sequence with other gold sequences when no. of sequence is 5.

## IV. CONCLUSIONS AND FUTURE SCOPE

The system developed shall provide a PN sequence (msequence) which is widely used in varied application areas like military applications, telecommunications etc. An attempt has been made in this work to generate m-sequence and then find autocorrelation of that series. Algorithm is developed in MATLAB. The comparison of simulated & measured values proves that sequences have excellent autocorrelation property. At the same time, for some basic character of m sequence such as autocorrelation and crosscorrelation simulation also give the code integer. The code



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is simple and efficient, and has strong skills

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